

Research Article

Track and Cut: Simultaneous Tracking and Segmentation of Multiple Objects with Graph Cuts

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Received 24 October 2007; Revised 26 March 2008; Accepted 14 May 2008

Recommended by Andrea Cavallaro

This paper presents a new method to both track and segment multiple objects in videos using min-cut/max-flow optimizations. We introduce objective functions that combine low-level pixel wise measures (color, motion), high-level observations obtained via an independent detection module, motion prediction, and contrast-sensitive contextual regularization. One novelty is that external observations are used without adding any association step. The observations are image regions (pixel sets) that can be provided by any kind of detector. The minimization of appropriate cost functions simultaneously allows “detection-before-track” tracking (track-to-observation assignment and automatic initialization of new tracks) and segmentation of tracked objects. When several tracked objects get mixed up by the detection module (e.g., a single foreground detection mask is obtained for several objects close to each other), a second stage of minimization allows the proper tracking and segmentation of these individual entities despite the confusion of the external detection module.

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1. INTRODUCTION

Visual tracking is an important and challenging problem in computer vision. Depending on applicative context under concern, it comes into various forms (automatic or manual initialization, single or multiple objects, still or moving camera, etc.), each of which being associated with an abundant literature. In a recent review on visual tracking [1], tracking methods are divided into three categories: point tracking, silhouette tracking, and kernel tracking. These three categories can be recast as “detect-before-track” tracking, dynamic segmentation and tracking based on distributions (color in particular). They are briefly described in Section 2.

In this paper, we address the problem of multiple objects tracking and segmentation by combining the advantages of the three classes of approaches. We suppose that, at each instant, the moving objects are approximately known thanks to some preprocessing algorithm. These moving objects form what we will refer to as the *observations* (as explained in Section 3). As possible instances of this detection module, we first use a simple background subtraction (the connected components of the detected foreground mask serve as high-

level observations) and then resort to a more complex approach [2] dedicated to the detection of moving objects in complex dynamic scenes. An important novelty of our method is that the use of external observations does not require the addition of a preliminary association step. The association between the tracked objects and the observations is conducted jointly with the segmentation and the tracking within the proposed minimization method.

At each time instant, tracked object masks are propagated using their associated optical flow, which provides predictions. Color and motion distributions are computed on the objects in the previous frame and used to evaluate individual pixel likelihoods in the current frame. We introduce, for each object, a binary labeling objective function that combines all these ingredients (low-level pixel wise features, high-level observations obtained via an independent detection module and motion predictions) with a contrast-sensitive contextual regularization. The minimization of each of these energy functions with min-cut/max-flow provides the segmentation of one of the tracked objects in the new frame. Our algorithm also deals with the introduction of new objects and their associated trackers.

When multiple objects trigger a single detection due to their spatial vicinity, the proposed method, as most detect-before-track approaches, can get confused. To circumvent this problem, we propose to minimize a secondary multilabel energy function, which allows the individual segmentation of concerned objects.

This article is an extended version of the work presented in [3]. They are however several noticeable improvements, which we now briefly summarize. The most important change concerns the description of the observations (Section 3.2). In [3], the observations were simply characterized by the mean value of their colors and motions. Here, as the object, they are described with mixtures of Gaussians, which obviously offers better modeling capabilities. Due to this new description, the energy function (whose minimization provides the mask of the tracked object) is different from the one in [3]. Also, we provide a more detailed justification of the various ingredients of the approach. In particular, we explain in Section 4.1 why each object has to be tracked independently, which was not discussed in [3]. Finally, we applied our method with the sophisticated multifeature detector we introduced in [2], while in [3] only a very simple background subtraction method was used as the source of object-based detection. This new detector can handle much more complex dynamic scenes but outputs only sparse clusters of moving points, not precise segmentation masks as background subtraction does. The use of this new detector demonstrates not only the genericity of our segmentation and tracking system, but also its ability to handle rough and inaccurate input measurements to produce good tracking.

The paper is organized as follows. In Section 2, a review of existing methods is presented. In Section 3, the notations are introduced and the objects and the observations are described. In Section 4, an overview of the method is given. The primary energy function associated to each tracked object is introduced in Section 5. The introduction of new objects is also explained in this section. The secondary energy function permitting the separation of objects wrongly merged in the first stage is presented in Section 6. Experimental results are finally reported in Section 7, where we demonstrate the ability of the method to detect, track, and correctly segment objects, possibly with partial occlusions and missing observations. The experiments also demonstrate that the second stage of minimization allows the segmentation of individual objects, when proximity in space (but also in terms of color and motion in case of more sophisticated detection) makes them merge at the object detection level.

2. EXISTING METHODS

In this section, we briefly describe the three categories (“detect-before-track,” dynamic segmentation, and “kernel tracking”) of existing tracking methods.

2.1. “Detect-before-track” methods

The principle of “detect-before-track” methods is to match the tracked objects with observations provided by an inde-

pendent detection module. Such a tracking can be performed with either deterministic or probabilistic methods.

Deterministic methods amount to matching by minimizing a distance between the object and the observations based on certain descriptors (position and/or appearance) of the object. The appearance—which can be, for example, the shape, the photometry, or the motion of the object—is often captured via empirical distributions. In this case, the histograms of the object and of a candidate observation are compared using an appropriate similarity measure, such as correlation, Bhattacharya coefficient, or Kullback-Leibler divergence.

The observations provided by a detection algorithm are often corrupted by noise. Moreover, the appearance (motion, photometry, shape) of an object can vary between two consecutive frames. Probabilistic methods provide means to take measurement uncertainties into account. They are often based on a state space model of the object properties and the tracking of one object is performed using a Bayesian filter (Kalman filtering [4], particle filtering [5]). Extension to multiple object tracking is also possible with such techniques, but a step of association between the objects and the observations must be added. The most popular methods for multiple object tracking in a “detect-before-track” framework are the multiple hypotheses tracking (MHT) and its probabilistic version (PMHT) [6, 7], and the joint probability data association filtering (JPDAF) [8, 9].

2.2. Dynamic segmentation

Dynamic segmentation aims at extracting successive segmentations over time. A detailed silhouette of the target object is thus sought in each frame. This is often done by making evolve the silhouette obtained in the previous frame toward a new configuration in current frame. The silhouette can either be represented by a set of parameters or by an energy function. In the first case, the set of parameters can be embedded into a state space model, which permits to track the contour with a filtering method. For example, in [10], several control points are positioned along the contour and tracked using a Kalman filter. In [11], the authors proposed to model the state with a set of splines and a few motion parameters. The tracking is then achieved with a particle filter. This technique was extended to multiple objects in [12].

Previous methods do not deal with the topology changes of an object silhouette. However, these changes can be handled when the object region is defined via a binary labeling of pixels [13, 14] or by the zero-level set of a continuous function [15, 16]. In both cases, the contour energy includes some temporal information in the form of either temporal gradients (optical flow) [17–19] or appearance statistics originated from the object and its surroundings in previous images [20, 21]. In [22], the authors use graph cuts to minimize such an energy functional. The advantages of min-cut/max-flow optimization are its low computational cost, the fact that it converges to the global minimum without getting stuck in local minima and that no prior on the global shape model is needed. They have also been used in [14] in

order to successively segment an object through time using a motion information.

2.3. “Kernel tracking”

The last group of methods aims at tracking a region of simple shape (often a rectangle or an ellipse) based on the conservation of its visual appearance. The best location of the region in the current frame is the one for which some feature distributions (e.g., color) are the closest to the reference ones for the tracked object. Two approaches can be distinguished: the ones that assume a short-term conservation of the appearance of the object and the ones that assume this conservation to last in time. The most popular method based on short-term appearance conservation is the so-called KLT approach [23], which is well suited to the tracking of small image patches. Among approaches based on long-term conservation, a very popular approach has been proposed by Comaniciu et al. [24, 25], where approximate “mean shift” iterations are used to conduct the iterative search. Graph cuts have also been used for illumination invariant kernel tracking in [26].

Advantages and limits of previous approaches

These three types of tracking techniques have different advantages and limitations and can serve different purposes. The “detect-before-track” approaches can deal with the entrance of new objects in the scene or the exit of existing ones. They use external observations that, if they are of good quality, might allow robust tracking. On the contrary, if they are of low quality the tracking can be deteriorated. Therefore, “detect-before-track” methods highly depend on the quality of the detection process. Furthermore, the restrictive assumption that one object can only be associated to at most one observation at a given instant is often made. Finally, this kind of tracking usually outputs bounding boxes only.

By contrast, silhouette tracking has the advantage of directly providing the segmentation of the tracked object. Representing the contour by a small set of parameters allows the tracking of an object with a relatively small computational time. On the other hand, these approaches do not deal with topology changes. Tracking by minimizing an energy functional allows the handling of topology changes but not always of occlusions (it depends on the dynamics used.) It can also be computationally inefficient and the minimization can converge to local minima of the energy. With the use of recent graph cuts techniques, convergence to the global minima is obtained at a modest computational cost. However, a limit of most silhouette tracking approaches is that they do not deal with the entrance of new objects in the scene or the exit of existing ones.

Finally, kernel tracking methods based on [24], thanks to their simple modeling of the global color distribution of target object, allow robust tracking at low cost in a wide range of color videos. However, they do not deal naturally with objects entering and exiting the field of view, and they do not

provide a detailed segmentation of the objects. Furthermore, they are not well adapted to the tracking of small objects.

3. OBJECTS AND OBSERVATIONS

We start the presentation of our approach by a formal definition of tracked objects and of observations.

3.1. Description of the objects

Let \mathcal{P} denote the set of N pixels of a frame from an input image sequence. To each pixel $s \in \mathcal{P}$ of the image at time t is associated a feature vector:

$$\mathbf{z}_t(s) = \left(\mathbf{z}_t^{(C)}(s), \mathbf{z}_t^{(M)}(s) \right), \quad (1)$$

where $\mathbf{z}_t^{(C)}(s)$ is a 3-dimensional vector in the color space and $\mathbf{z}_t^{(M)}(s)$ is a 2-dimensional vector measuring the apparent motion (optical flow). We consider a chrominance color space (here we use the YUV space, where Y is the luminance, U and V the chrominances) as the objects that we track often contain skin, which is better characterized in such a space [27, 28]. Furthermore, a chrominance space has the advantage of having the three channels, Y, U, and V, uncorrelated. The optical flow vectors are computed using an incremental multiscale implementation of Lucas and Kanade algorithm [29]. This method does not hold for pixels with insufficiently contrasted surroundings. For these pixels, the motion is not computed and color constitutes the only low-level feature. Therefore, although not always explicit in the notation for the sake of conciseness, one should bear in mind that we only consider a sparse motion field. The set of pixels with an available motion vector will be denoted as $\Omega \subset \mathcal{P}$.

We assume that, at time t , k_t objects are tracked. The i th object at time t , $i = 1 \dots k_t$, is denoted as $\mathcal{O}_t^{(i)}$ and is defined as a set of pixels, $\mathcal{O}_t^{(i)} \subset \mathcal{P}$. The pixels of a frame that do not belong to the object $\mathcal{O}_t^{(i)}$ constitute its “background.” Both the objects and the backgrounds will be represented by a distribution that combines motion and color information. Each distribution is a mixture of Gaussians—All mixtures of Gaussians in this work are fitted using the expectation-maximization (EM) algorithm. For object i at instant t , this distribution, denoted as $p_t^{(i)}$, is fitted to the set of values $\{\mathbf{z}_t(s)\}_{s \in \mathcal{O}_t^{(i)}}$. This means that the mixture of Gaussians of object i is recomputed at each time instant, which allows our approach to be robust to progressive illumination changes. For computational cost reasons, one could instead use a fixed reference distribution or a progressive update of the distribution (which is not always a trivial task [30, 31]).

We consider that motion and color information is independent. Hence, the distribution $p_t^{(i)}$ is the product of a color distribution, $p_t^{(i,C)}$ (fitted to the set of values $\{\mathbf{z}_t^{(C)}(s)\}_{s \in \mathcal{O}_t^{(i)}}$) and a motion distribution $p_t^{(i,M)}$ (fitted to the set of values $\{\mathbf{z}_t^{(M)}(s)\}_{s \in \mathcal{O}_t^{(i)} \cap \Omega}$). Under this independence assumption for color and motion, the likelihood of individual pixel feature $\mathbf{z}_t(s)$ according to previous joint model is

$$p_t^{(i)}(\mathbf{z}_t(s)) = p_t^{(i,C)}(\mathbf{z}_t^{(C)}(s)) p_t^{(i,M)}(\mathbf{z}_t^{(M)}(s)), \quad (2)$$



FIGURE 1: Observations obtained with background subtraction: (a) reference frame, (b) current frame, and (c) result of background subtraction (pixels in black are labeled as foreground) and derived object detections (indicated with red bounding boxes).

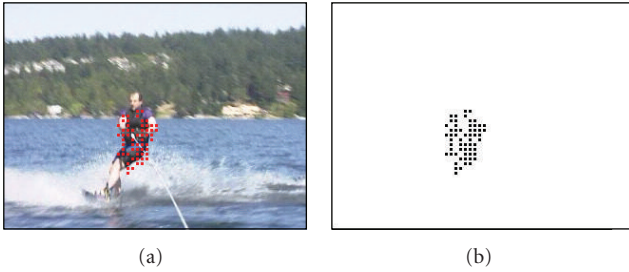


FIGURE 2: Observations obtained with [2] on a water skier sequence shot by a moving camera: (a) detected moving clusters superposed on the current frame and (b) mask of pixels characterizing the observation.

when $s \in \mathcal{O}_t^{(i)} \cap \Omega$. As we only consider a sparse motion field, color distribution only is taken into account for pixels with no motion vector: $p_t^{(i)}(\mathbf{z}_t(s)) = p_t^{(i,C)}(\mathbf{z}_t^{(C)}(s))$ if $s \in \mathcal{O}_t^{(i)} \setminus \Omega$.

The background distributions are computed in the same way. The distribution of the background of object i at time t , denoted as $q_t^{(i)}$, is a mixture of Gaussians fitted to the set of values $\{\mathbf{z}_t(s)\}_{s \in \mathcal{P} \setminus \mathcal{O}_t^{(i)}}$. It also combines motion and color information:

$$q_t^{(i)}(\mathbf{z}_t(s)) = q_t^{(i,C)}(\mathbf{z}_t^{(C)}(s))q_t^{(i,M)}(\mathbf{z}_t^{(M)}(s)). \quad (3)$$

3.2. Description of the observations

Our goal is to perform both segmentation and tracking to get the object $\mathcal{O}_t^{(i)}$ corresponding to the object $\mathcal{O}_{t-1}^{(i)}$ of previous frame. Contrary to sequential segmentation techniques [13, 32, 33], we bring in object-level “observations.” We assume that, at each time t , there are m_t observations. The j th, $i = 1 \dots m_t$, observation at time t is denoted as $\mathcal{M}_t^{(j)}$ and is defined as a set of pixels, $\mathcal{M}_t^{(j)} \subset \mathcal{P}$.

As objects and backgrounds, observation j at time t is represented by a distribution, denoted as $\rho_t^{(j)}$, which is a mixture of Gaussians combining color and motion information. The mixture is fitted to the set $\{\mathbf{z}_t(s)\}_{s \in \mathcal{M}_t^{(j)}}$ and is defined as

$$\rho_t^{(j)}(\mathbf{z}_t(s)) = \rho_t^{(j,C)}(\mathbf{z}_t^{(C)}(s))\rho_t^{(j,M)}(\mathbf{z}_t^{(M)}(s)). \quad (4)$$

The observations may be of various kinds (e.g., obtained by a class-specific object detector, or motion/color detectors). Here, we will consider two different types of observations.

3.2.1. Background subtraction

The first type of observations comes from a preprocessing step of background subtraction. Each observation amounts to a connected component of the foreground detection map obtained by thresholding the difference between a reference frame and the current frame and by removing small regions (Figure 1). The connected components are obtained using the “gap/mountain” method described in [34].

In the first frame, the tracked objects are initialized as the observations themselves.

3.2.2. Moving objects detection in complex scenes

In order to be able to track objects in more complex sequences, we will use a second type of objects detector. The method considered is the one from [2] that can be decomposed in three main steps. First, a grid \mathcal{G} of moving pixels having valid motion vectors is selected. Each point is described by its position, its color, and its motion. Then these points are partitioned based on a mean shift algorithm [35], leading to several moving clusters. Finally, segmentation of the objects are obtained from the moving clusters by minimizing appropriate energy functions with graph cuts. This last step can be avoided here. Indeed, as we here propose a method that simultaneously track and segment objects, the observations do not need to be fully segmented objects. Therefore, the observations will simply be the detected clusters of moving points (Figure 2).

The segmentation part of the detection preprocessing will only be used when initializing new objects to be tracked. When the system declares that a new tracker should be created from a given observation, the tracker is initialized with the corresponding segmented detected object.

In this detection method, motion vectors are only computed on the points of sparse grid \mathcal{G} . Therefore, in our tracking algorithm, when using this type of observations, we will stick to this sparse grid as the set of pixels that are described both by their color and by their motion ($\Omega = \mathcal{G}$).

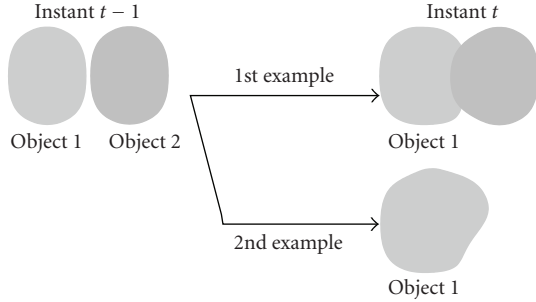


FIGURE 3: Example illustrating why the objects are tracked independently.

4. PRINCIPLES OF THE TRACK AND CUT SYSTEM

Before getting to the details of our approach, we start by presenting its main principles. In particular, we explain why it is decomposed into two steps (first a segmentation/tracking method and then, when necessary, a further segmentation step) and why each object is tracked independently.

4.1. Tracking each object independently

We propose in this work a tracking method that is based on energy minimizations. Minimizing an energy with min-cut/max-flow in capacity graphs [36] permits to assign a label to each pixel of an image. As in [37], the labeling of one pixel will here depend both on the agreement between the appearance at this pixel and the objects appearances and on the similarity between this pixel and its neighbors. Indeed, a binary smoothness term that encourages two neighboring pixels with similar appearances to get the same label is added to the energy function.

In our tracking scheme, we wish to assign a label corresponding to one of the tracked objects or to the background to each pixel of the image. By using a multilabel energy function (each label corresponding to one object), all objects would be directly tracked simultaneously by minimizing a single energy function. However, we prefer not to use such a multilabel energy in general, and track each object independently. Such a choice comes from an attempt to distinguish the merging of several objects from the occlusions of some objects by another one, which cannot be done using a multilabel energy function. Let us illustrate this problem on an example. Assume two objects having similar appearances are tracked. We are going to analyze and compare the two following scenarios (described in Figure 3).

On the one hand, we suppose that the two objects become connected in the image plane at time t and, on the other hand, that one of the objects occludes the second one at time t .

First, suppose that these two objects are tracked using a multilabel energy function. Since the appearances of the objects are similar, when they get side by side (first case), the minimization will tend to label all the pixels in the same way (due to the smoothness term). Hence, each pixel will probably be assigned the same label, corresponding to

only one of the tracked objects. In the second case, when one object occludes the other one, the energy minimization leads to the same result: all the pixels have the same label. Therefore, it is possible for these two scenarios to be confused.

Assume now that each object is tracked independently by defining one energy function per object (each pixel is then associated to k_{t-1} labels). For each object, the final label of a pixel is either “object” or “background.” For the first case, each pixel of the two objects will be, at the end of the two minimizations, labeled as “object.” For the second case, the pixels will be labeled as “object” when the minimization is done for the occluding object and as “background” for the occluded one. Therefore, by defining one energy function per object, we are able to differentiate the two cases. Of course, for the first case, the obtained result is not the wanted one: the pixels get the same label which means that the two objects have merged. In order to keep distinguishing the two objects, we equip our tracking system with an additional separation step in case objects get merged.

The principles of the tracking, including the separation of merged objects, are explained in next subsections.

4.2. Principle of the tracking method

The principle of our algorithm is as follows. A prediction $\mathcal{O}_{t|t-1}^{(i)} \subset \mathcal{P}$ is made for each object i of time $t-1$. We denote as $\mathbf{d}_{t-1}^{(i)}$ the mean, over all pixels of the object at time $t-1$, of optical flow values:

$$\mathbf{d}_{t-1}^{(i)} = \frac{\sum_{s \in \mathcal{O}_{t-1}^{(i)} \cap \Omega} \mathbf{z}_{t-1}^{(M)}(s)}{|\mathcal{O}_{t-1}^{(i)} \cap \Omega|}. \quad (5)$$

The prediction is obtained by translating each pixel belonging to $\mathcal{O}_{t-1}^{(i)}$ by this average optical flow:

$$\mathcal{O}_{t|t-1}^{(i)} = \left\{ s + \mathbf{d}_{t-1}^{(i)}, s \in \mathcal{O}_{t-1}^{(i)} \right\}. \quad (6)$$

Using this prediction, the new observations and the distribution $p_t^{(i)}$ of $\mathcal{O}_{t-1}^{(i)}$, an energy function is built. This energy is minimized using min-cut/max-flow algorithm [36], which gives the new segmented object at time t , $\mathcal{O}_t^{(i)}$. The minimization also provides the correspondences of the object with all the available observations, which simply leads to the creation of new trackers when one or several observations at current instant remain unassociated. Our tracking algorithm is diagrammatically summarized in Figure 4.

4.3. Separating merged objects

At the end of the tracking step, several objects can be merged, that is, the segmentations for different objects overlap: $\exists(i, j) : \mathcal{O}_t^{(i)} \cap \mathcal{O}_t^{(j)} \neq \emptyset$. In order to keep tracking each object separately, the merged objects must be separated. This will be done by adding a multilabel energy minimization.

5. ENERGY FUNCTIONS

We define one tracker per object. To each tracker corresponds, for each frame, one graph and one energy function that is minimized using the min-cut/max-flow algorithm [36]. Nodes and edges of the graph can be seen in Figure 5. This figure will be further explained in Section 5.1. In all our work, we consider an 8-neighborhood system. However, for the sake of clarity, only a 4-neighborhood is used in all the figures representing a graph.

5.1. Graph

The undirected graph $G_t = (\mathcal{V}_t, \mathcal{E}_t)$ at time t is defined as a set of nodes \mathcal{V}_t and a set of edges \mathcal{E}_t . The set of nodes is composed of two subsets. The first subset is the set of the N pixels of the image grid \mathcal{P} . The second subset corresponds to the observations: to each observation mask $\mathcal{M}_t^{(j)}$ is associated a node $n_t^{(j)}$. We call these nodes “observation nodes.” The set of nodes thus reads $\mathcal{V}_t = \mathcal{P} \cup \{n_t^{(j)}, j = 1 \dots m_t\}$. The set of edges is decomposed as follows: $\mathcal{E}_t = \mathcal{E}_{\mathcal{P}} \cup_{j=1}^{m_t} \mathcal{E}_{\mathcal{M}_t^{(j)}}$, where $\mathcal{E}_{\mathcal{P}}$ is the set of all unordered pairs $\{s, r\}$ of neighboring elements of \mathcal{P} , and $\mathcal{E}_{\mathcal{M}_t^{(j)}}$ is the set of unordered pairs $\{s, n_t^{(j)}\}$, with $s \in \mathcal{M}_t^{(j)}$.

Segmenting the object $\mathcal{O}_t^{(i)}$ amounts to assigning a label $l_{s,t}^{(i)}$, either background, “bg,” or object, “fg,” to each pixel node s of the graph. Associating observations to tracked objects amounts to assigning a binary label $l_{j,t}^{(i)}$ (“bg” or “fg”) to each observation node $n_t^{(j)}$ (for the sake of clarity, the notation $l_{j,t}^{(i)}$ has been preferred to $l_{n_t^{(j)},t}^{(i)}$). The set of all the node labels is denoted as $L_t^{(i)}$.

5.2. Energy

An energy function is defined for each object i at each instant t . It is composed of data terms $R_{s,t}^{(i)}$ and binary smoothness terms $B_{s,r,t}^{(i)}$:

$$E_t^{(i)}(L_t^{(i)}) = \sum_{s \in \mathcal{V}_t} R_{s,t}^{(i)}(l_{s,t}^{(i)}) + \sum_{\{s,r\} \in \mathcal{E}_t} B_{\{s,r\},t}^{(i)}(1 - \delta(l_{s,t}^{(i)}, l_{r,t}^{(i)})), \quad (7)$$

where δ is the characteristic function defined as

$$\delta(l_s, l_r) = \begin{cases} 1 & \text{if } l_s = l_r, \\ 0 & \text{else.} \end{cases} \quad (8)$$

In order to simplify the notations, we omit object index i in the rest of this section.

5.2.1. Data term

The data term only concerns the pixel nodes lying in the predicted regions and the observation nodes. For all the other pixel nodes, labeling will only be controlled by the neighbors

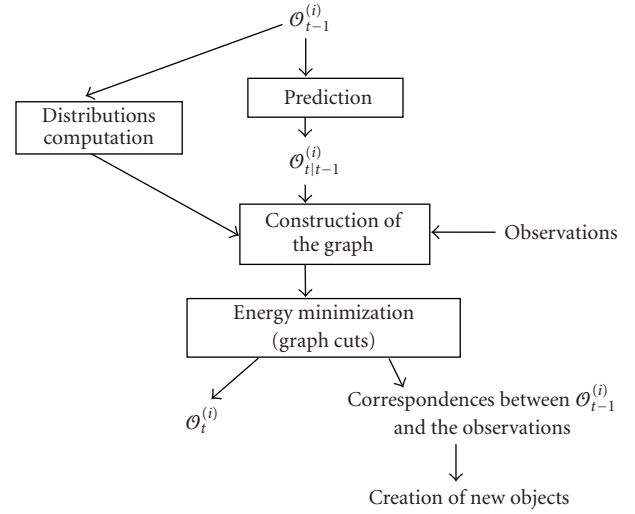


FIGURE 4: Principle of the algorithm.

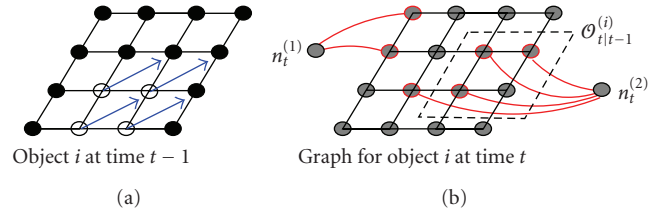


FIGURE 5: Description of the graph. The left figure is the result of the energy minimization at time $t - 1$. White nodes are labeled as object and black nodes as background. The optical flow vectors for the object are shown in blue. The right figure shows the graph at time t . Two observations are available, each of which giving rise to a special “observation” node. The pixel nodes circled in red correspond to the masks of these two observations. The dashed box indicates the predicted mask.

via binary terms. More precisely, the first part of energy in (7) reads

$$\sum_{s \in \mathcal{V}_t} R_{s,t}(l_{s,t}) = \alpha_1 \sum_{s \in \mathcal{O}_{t|t-1}} -\ln(p_1(s, l_{s,t})) + \alpha_2 \sum_{j=1}^{m_t} d_2(n_t^{(j)}, l_{j,t}). \quad (9)$$

Segmented object at time t should be similar, in terms of motion and color, to the preceding instance of this object at time $t - 1$. To exploit this consistency assumption, the distribution of the object, p_{t-1} (2), and of the background, q_{t-1} (3), from previous image, is used to define the likelihood p_1 , within predicted region as

$$p_1(s, l) = \begin{cases} p_{t-1}(\mathbf{z}_t(s)) & \text{if } l = \text{“fg”}, \\ q_{t-1}(\mathbf{z}_t(s)) & \text{if } l = \text{“bg”}. \end{cases} \quad (10)$$

In the same way, an observation should be used only if it is likely to correspond to the tracked object. To evaluate the similarity of observation j at time t and object i at previous time, a comparison between the distributions p_{t-1}

and $\rho_t^{(j)}$ (4) and between q_{t-1} and $\rho_t^{(j)}$ must be performed through the computation of a distance measure. A classical distance to compare two mixtures of Gaussians, G_1 and G_2 , is the Kullback-Leibler divergence [38], defined as

$$\text{KL}(G_1, G_2) = \int G_1(\mathbf{x}) \log \frac{G_1(\mathbf{x})}{G_2(\mathbf{x})} d\mathbf{x}. \quad (11)$$

This asymmetric function measures how well distribution G_2 mimics the variations of distribution G_1 . Here, we want to know if the observations belongs to the object or to the background but not the opposite, and therefore we will measure if one or several observations belong to one object. The data term d_2 is then

$$d_2(s, l) = \begin{cases} \text{KL}(\rho_t^{(j)}, p_{t-1}) & \text{if } l = \text{“fg”} \\ \text{KL}(\rho_t^{(j)}, q_{t-1}) & \text{if } l = \text{“bg”} \end{cases} \quad (12)$$

Two constants α_1 and α_2 are included in the data term in (9) to give more or less influence to the observations. In our experiments, they were both fixed to 1.

5.2.2. Binary term

Following [37], the binary term between neighboring pairs of pixels $\{s, r\}$ of \mathcal{P} is based on color gradients and has the form

$$B_{\{s,r\},t} = \lambda_1 \frac{1}{\text{dist}(s,r)} e^{-\frac{\|z_t^{(C)}(s) - z_t^{(C)}(r)\|^2}{\sigma_T^2}}. \quad (13)$$

As in [39], the parameter σ_T is set to $\sigma_T = 4 \cdot \langle (z_t^{(C)}(s) - z_t^{(C)}(r))^2 \rangle$, where $\langle \cdot \rangle$ denotes expectation over a box surrounding the object.

For graph edges between one pixel node and one observation node, the binary term depends on the distance between the color of the observation and the pixel color. More precisely, this term discourages the cut of an edge linking one pixel to an observation node, if this pixel has a high probability (through its color and motion) to belong to the corresponding observation. This binary term is then computed as

$$B_{\{s,n_t^{(j)}\},t} = \lambda_2 \rho_t^{(j)} (z_t^{(C)}(s)). \quad (14)$$

Parameters λ_1 and λ_2 are discussed in the experiments.

5.2.3. Energy minimization

The final labeling of pixels is obtained by minimizing, with the min-cut/max-flow algorithm proposed in [40], the energy defined above:

$$\hat{L}_t^{(i)} = \arg \min_{L_t^{(i)}} E_t^{(i)}(L_t^{(i)}). \quad (15)$$

This labeling finally gives the segmentation of the i th object at time t as

$$\mathcal{O}_t^{(i)} = \{s \in \mathcal{P} : \hat{L}_{s,t}^{(i)} = \text{“fg”}\}. \quad (16)$$

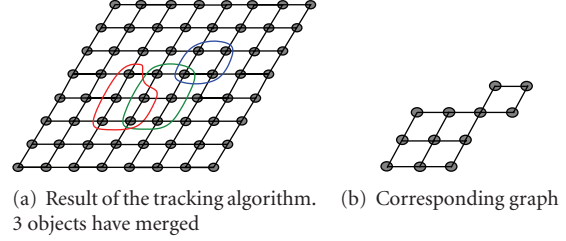


FIGURE 6: Graph example for the segmentation of merged objects.

5.3. Creation of new objects

One advantage of our approach lies in its ability to jointly manipulate pixel labels and track-to-detection assignment labels. This allows the system to track and segment the objects at time t , while establishing the correspondences between an object currently tracked and all the approximative candidate objects obtained by detection in the current frame. If, after the energy minimization for an object i , an observation node $n_t^{(j)}$ is labeled as “fg” ($\hat{L}_{t,j}^{(i)} = \text{“fg”}$) it means that there is a correspondence between the i th object and the j th observation. Conversely, if the node is labeled as “bg,” the object and the observation are not associated.

If for all the objects ($i = 1, \dots, k_{t-1}$), an observation node is labeled as “bg” ($\forall i, \hat{L}_{t,j}^{(i)} = \text{“bg”}$), then the corresponding observation does not match any object. In this case, a new object is created and initialized with this observation. The number of tracked objects becomes $k_t = k_{t-1} + 1$, and the new object is initialized as

$$\mathcal{O}_t^{(k_t)} = \mathcal{M}_t^{(j)}. \quad (17)$$

In practice, the creation of a new object will be only validated, if the new object is associated to at least one observation at time $t + 1$, that is, if $\exists j \in \{1, \dots, m_{t+1}\}$ such that $\hat{L}_{j,t+1}^{(k_t)} = \text{“fg”}$.

6. SEGMENTING MERGED OBJECTS

Assume now that the results of the segmentations for different objects overlap, that is to say

$$\exists (i, j), \mathcal{O}_t^{(i)} \cap \mathcal{O}_t^{(j)} \neq \emptyset. \quad (18)$$

In this case, we propose an additional step to determine whether these segmentation masks truly correspond to the same object or if they should be separated. At the end of this step, each pixel must belong to only one object.

Let us introduce the notation

$$\mathcal{F} = \{i \in \{1, \dots, k_t\} \mid \exists j \neq i \text{ such that } \mathcal{O}_t^{(i)} \cap \mathcal{O}_t^{(j)} \neq \emptyset\}. \quad (19)$$

A new graph $\tilde{G}_t = (\tilde{\mathcal{V}}_t, \tilde{\mathcal{E}}_t)$ is created, where $\tilde{\mathcal{V}}_t = \cup_{i \in \mathcal{F}} \mathcal{O}_t^{(i)}$ and $\tilde{\mathcal{E}}_t$ is composed of all unordered pairs of neighboring pixel nodes in $\tilde{\mathcal{V}}_t$. An example of such a graph is presented in Figure 6.

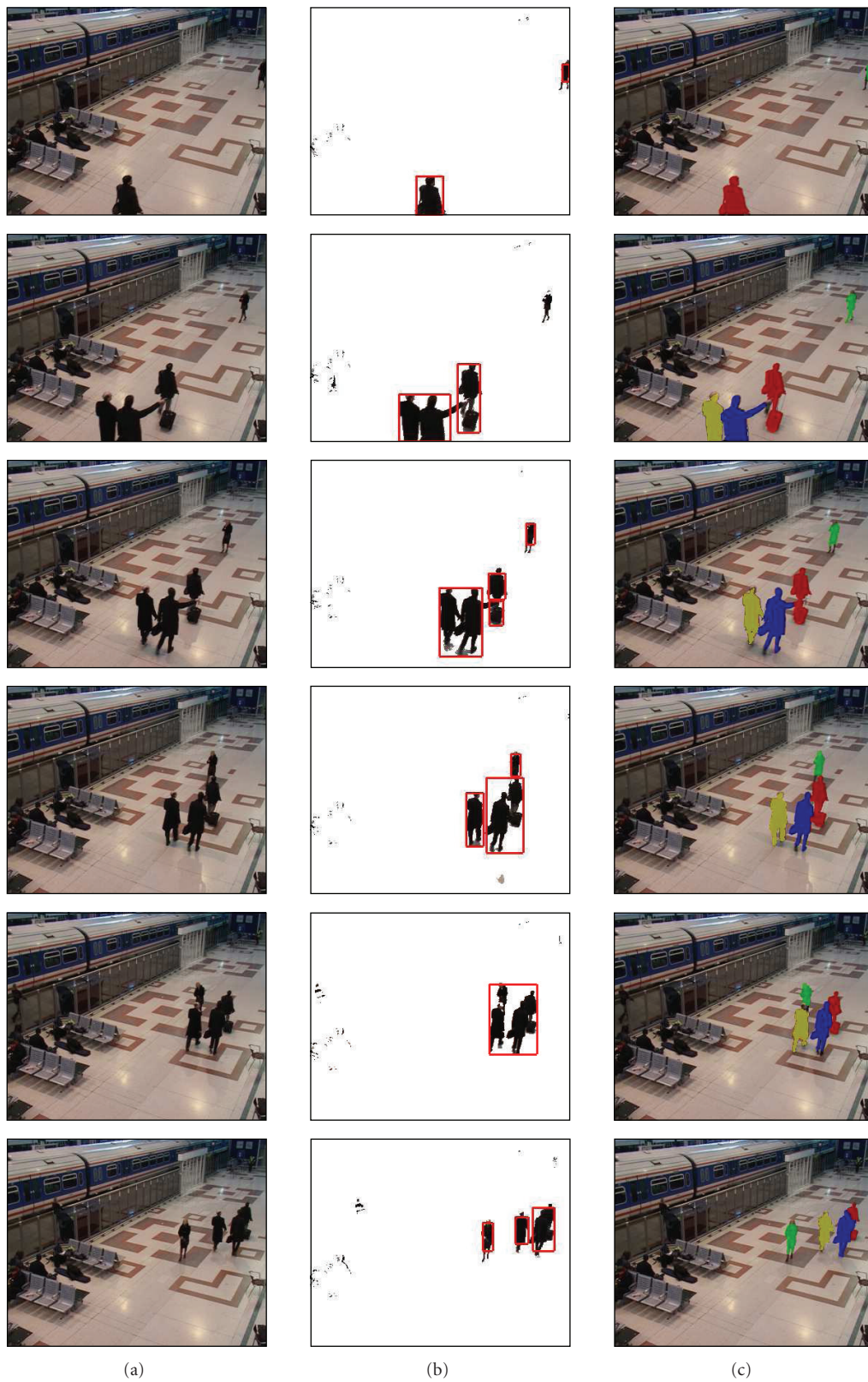


FIGURE 7: Results on sequence from PETS 2006 (frames 81, 116, 146, 176, 206, and 248): (a) original frames, (b) result of simple background subtraction and extracted observations, and (c) tracked objects on current frame using the primary and the secondary energy functions.

The goal is then to assign to each node s of $\tilde{\mathcal{V}}_t$ a label $\psi_s \in \mathcal{F}$. Defining $\tilde{\mathcal{L}} = \{\psi_s, s \in \tilde{\mathcal{V}}_t\}$ the labeling of $\tilde{\mathcal{V}}_t$, a new energy is defined as

$$\begin{aligned} \tilde{E}_t(\tilde{\mathcal{L}}) = & \sum_{s \in \tilde{\mathcal{V}}_t} -\ln(p_3(s, \psi_s)) \\ & + \lambda_3 \sum_{\{s,r\} \in \tilde{\mathcal{E}}_t} \frac{1}{\text{dist}(s,r)} e^{-\|\mathbf{z}_s^{(C)} - \mathbf{z}_r^{(C)}\|^2 / \sigma_3^2} (1 - \delta(\psi_s, \psi_r)). \end{aligned} \quad (20)$$

The parameter σ_3 is here set as $\sigma_3 = 4 \cdot \langle (\mathbf{z}_t(s)^{(i,C)} - \mathbf{z}_t(r)^{(i,C)})^2 \rangle$ with the averaging being over $i \in \mathcal{F}$ and $\{s,r\} \in \tilde{\mathcal{E}}_t$. The fact that several objects have been merged shows that their respective feature distributions at previous instant did not permit to distinguish them. A way to separate them is then to increase the role of the prediction. This is achieved by choosing function p_3 as

$$p_3(s, \psi) = \begin{cases} p_{t-1}^{(\psi)}(\mathbf{z}_t(s)) & \text{if } s \notin \mathcal{O}_{t|t-1}^{(\psi)}, \\ 1 & \text{otherwise.} \end{cases} \quad (21)$$

This multilabel energy function is minimized using the expansion move algorithm [36, 41]. The convergence to the global optimal solution with this algorithm cannot be proved. Only the convergence to a locally optimal solution is guaranteed. Still, in all our experiments, this method gave satisfactory results. After this minimization, the objects $\mathcal{O}_t^{(i)}$, $i \in \mathcal{F}$ are updated.

7. EXPERIMENTAL RESULTS

This section presents various results of joint tracking/segmentation, including cases, where merged objects have to be separated in a second step. First, we will consider a relatively simple sequence, with static background, in which the observations are obtained by background subtraction (Section 3.2.1). Next, the tracking method will be combined to the moving objects detector introduced in [2] (Section 3.2.2).

7.1. Tracking objects detected with background subtraction

In this section, tracking results obtained on a sequence from the PETS 2006 data corpus (sequence 1 camera 4) are presented. They are followed by an experimental analysis of the first energy function (7). More precisely, the influence of each of its four terms (two for the data part and two for the smoothness part) is shown in the same image.

7.1.1. A first tracking result

We start by demonstrating the validity of the approach, including its robustness to partial occlusions and its ability to segment individually objects that were initially merged.

Following [39], the parameter λ_3 was set to 20. However, parameters λ_1 and λ_2 had to be tuned by hand to get better

results ($\lambda_1 = 10, \lambda_2 = 2$). Also, the number of classes for the Gaussian mixture models was set to 10.

First results (Figure 7) demonstrate the good behavior of our algorithm even in the presence of partial occlusions and of object fusion. Observations, obtained by subtracting a reference frame (frame 10 shown in Figure 1(a)) to the current one, are visible in the second column of Figure 7, the third column contains the segmentation of the objects with the subsequent use of the second energy function. In frame 81, two objects are initialized using the observations. Note that the connected component extracted with the ‘‘gap/mountain’’ method misses the legs for the person in the upper right corner. While this has an impact on the initial segmentation, the legs are recovered in the final segmentation as soon as the following frame.

Let us also underline the fact that the proposed method easily deals with the entrance of new objects in the scene. This result also shows the robustness of our method to partial occlusions. For example, partial occlusions occur when the person at the top passes behind the three other ones (frames 176 and 206). Despite the similar color of all the objects, this is well handled by the method, as the person is still tracked when the occlusion stops (frame 248).

Finally note that even if from frame 102, the two persons at the bottom correspond to only one observation and have a similar appearance (color and motion), our algorithm tracks each person separately (frames 116, 146) thanks to the second energy function. In Figure 8, we show in more details the influence of the second energy function by comparing the results obtained with and without it. Before frame 102, the three persons at the bottom generate three distinct observations, while, passed this instant, they correspond to only one or two observations. Even if the motions and colors of the three persons are very close, the use of the second multilabel energy function allows their separation.

7.1.2. A qualitative analysis of the first energy function

We now propose an analysis of the influence on the results of each of the four terms of the energy defined in (7). The weight of each of these terms is controlled by a parameter. Indeed, we remind that the complete energy function has been defined as

$$\begin{aligned} E_t(L_t) = & \sum_{s \in \mathcal{V}_t} \left[\alpha_1 \sum_{s \in \mathcal{O}_{t|t-1}} -\ln(P_1(s, l_{s,t})) + \alpha_2 \sum_{j=1}^{m_t} d_2(n_t^{(j)}, l_{j,t}) \right] \\ & + \lambda_1 \sum_{\{s,r\} \in \mathcal{E}_\varphi} B_{\{s,r\},t} (1 - \delta(l_{s,t}, l_{r,t})) \\ & + \lambda_2 \sum_{j=1}^{m_t} \sum_{\{s,r\} \in \mathcal{E}_{\mathcal{M}_t^{(j)}}} B_{\{s,r\},t} (1 - \delta(l_{s,t}, l_{r,t})). \end{aligned} \quad (22)$$

To show the influence of each term, we successively set one of the parameters λ_1 , λ_2 , α_1 , and α_2 to zero. The results on a frame from the PETS sequence are visible on Figure 9. Figure 9(a) presents the original image, Figure 9(b) presents the extracted observation after background subtraction, and

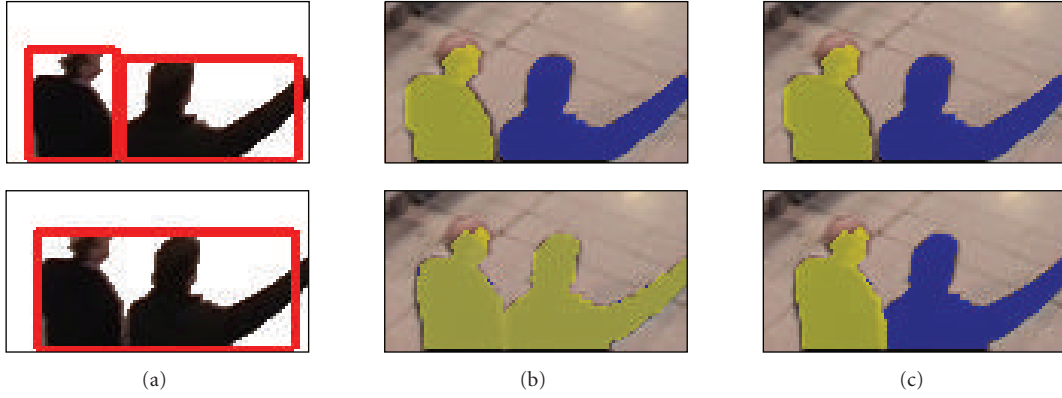


FIGURE 8: Separating merged objects with the secondary minimization (frames 101 and 102): (a) result of simple background subtraction and extracted observations, (b) segmentations with the first energy functions only, and (c) segmentation after postprocessing with the secondary energy function.

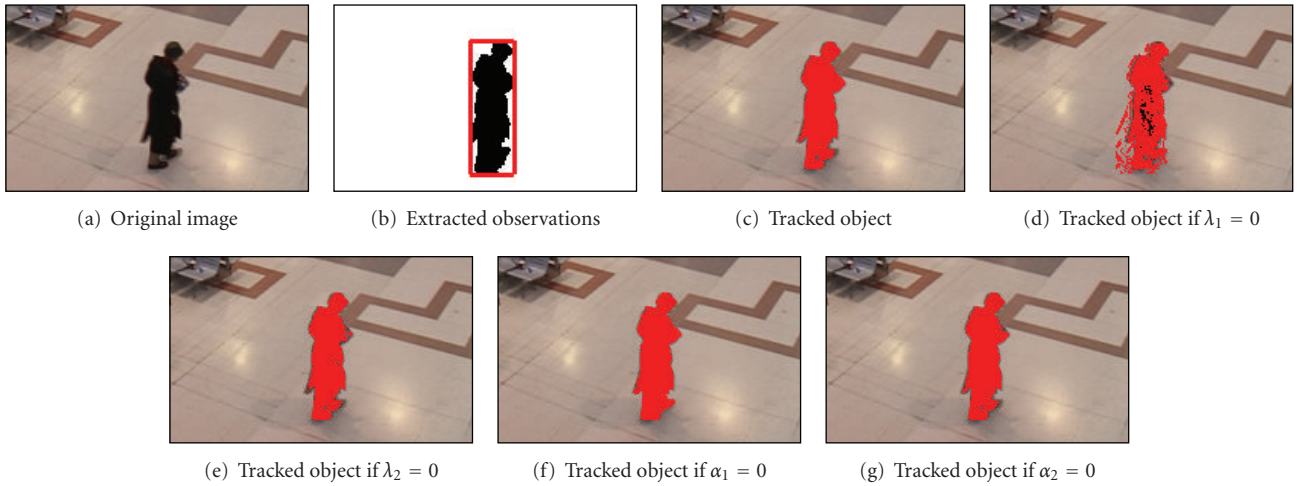


FIGURE 9: Influence of each term of the first energy function on the frame 820 of the PETS sequence.

Figure 9(c) presents the tracked object when using the complete energy equation (22) with $\lambda_1 = 10$, $\lambda_2 = 2$, $\alpha_1 = 1$, and $\alpha_2 = 2$.

If the parameter λ_1 is equal to zero, it means that no spatial regularization is applied to the segmentation. The final mask of the object then only depends on the probability of each pixel to belong to the object, the background, and the observations. That is the reason why the object is not well segmented in Figure 9(d). If $\lambda_2 = 0$, the observations do not influence the segmentation of the object. As can be seen in Figure 9(e), it can lead to a slight undersegmentation of the object. In the case that $\alpha_2 = 0$, the labeling of an observation node only depends on the labels of the pixels belonging to this observation. Therefore, this term mainly influences the association between the observations and the tracked objects. Nevertheless, as can be seen in Figure 9(g), it also slightly modifies the mask of a tracked object, and switching it off might produce an undersegmentation of the object. Finally, when $\alpha_1 = 0$, the energy minimization yields to the spatial regularization of the observation mask thanks to the binary

smoothness term. The mask of the object then stops on the strong contours but does not take into account the color and motion of the pixels belonging to the prediction. In Figure 9(f), this leads to an oversegmentation of the object compared to the segmentation of the object at previous time instants.

This experiment illustrates that each term of the energy function plays a role of its own on the final segmentation of the tracked objects.

7.2. Tracking objects in complex scenes

We are now showing the behavior of our tracking algorithm when the sequences are more complex (dynamic background, moving camera, etc.). For each sequence, the observations are the moving clusters detected with the method of [2]. In all this subsection, the parameter λ_3 was set to 20, λ_1 to 10, and λ_2 to 1.

The first result is on a water skier sequence (Figure 10).

For each image, the moving clusters and the masks of the tracked objects are superimposed on the original



FIGURE 10: Results on a water skier sequence. The observations are moving clusters detected with the method in [2]. At each time instant, the observations are shown in the left image, while the masks of the tracked objects are shown in the right image.

image. The proposed tracking method permits to correctly track the water skier (or more precisely his wet suit) all along the sequence, despite fast trajectory changes, drastic deformations, and moving surroundings. As can be seen in the figure (e.g., at time 58), the detector sometimes fails to detect the skier. No observations are available in these cases. However, by using the prediction of the object, our method handles well such situations and keeps tracking and segmenting correctly the skier. This shows the robustness of the algorithm to missing observations. However, if some observations are missing for several consecutive frames, the segmentation can get deteriorated. Conversely, this means that the incorporation of the observations produced by the detection module enables to get better segmentations than when using only predictions. On several frames, moving clusters are detected in the water. Nevertheless, no objects are created in concerned areas. The reason is that the creation of a new object is only validated, if the new object is associated to at least one observation in the following frame. This never happened in the sequence.

We end by showing results on a driver sequence (Figure 11). The first object detected and tracked is the face. Once again, tracking this object shows the robustness of our method to missing observations. Indeed, even if from frame 19, the face does not move and therefore is not detected, the algorithm keeps tracking and segmenting it correctly until the driver starts turning it. The most important result on this sequence is the tracking of the hands. In image 39, the masks of the two hands are merged: they have a few pixels in common. The step of segmentation of merged objects is then applied and allows the correct separation of the two masks, which permits to keep tracking these two objects separately. Finally, as can be seen on frame 57, our method deals well with the exit of an object from the scene.

8. CONCLUSION

In this paper, we have presented a new method that simultaneously segments and tracks multiple objects in videos. Predictions along with observations composed of detected objects are combined in an energy function which



FIGURE 11: Results on a driver sequence. The observations are moving clusters detected with the method in [2]. At each time instant, the observations are shown in the left image, while the masks of the tracked objects are shown in the right image.

is minimized with graph cuts. The use of graph cuts permits the segmentation of the objects at a modest computational cost, leaving the computational bottleneck at the level of the detection of objects and of the computation of GMMs.

An important novelty is the use of observation nodes in the graph which gives better segmentations but also enables the direct association of the tracked objects to the observations (without adding any association procedure). The observations used in this paper are obtained firstly by a simple background subtraction based on a single reference frame and secondly by a more sophisticated moving object detector. Note however that any object detection method could be used as well, with no change to the approach, as soon as the observations can be represented by a set of pixels.

The proposed method combines the main advantages of each of the three categories of existing methods presented in Section 2. It deals with the entrance of new objects in the scene and the exit of existing ones, as “detect-before-track” methods do; as silhouette tracking methods, the energy minimization directly outputs the segmentation mask of the objects; it allows robust tracking in a wide range of color

videos thanks to the use of global distributions, as with other kernel tracking algorithms.

As shown in the experiments, the algorithm is robust to partial occlusions and to missing observations and does not require accurate observations to provide good segmentations. Also, several observations can correspond to one object (water skier sequence) and several objects can correspond to one observation (PETS sequence). Thanks to the use of a second multilabel energy function, our method allows individual tracking and segmentation of objects which were not distinguished from each other in the first stage.

As we use feature distributions of objects at previous time to define current energy functions, our method handles progressive illumination changes but breaks down in extreme cases of abrupt illumination changes. However, by adding an external detector of such changes, we could circumvent this problem by keeping only the prediction and by updating the reference frame when the abrupt change occurs.

Also, other cues, such as shapes, could probably be added to improve the results. The problem would then be to introduce such a global feature into the energy function.

As it turns out, it is difficult to add a global term in an energy function that is minimized by graph cuts. Another solution could be to select a compact characterization of the shape (e.g., pose parameters [42], ellipse parameters [43], normalized central moments [44], or some top-down knowledge [45]) and to add a term such as the face energy term proposed in [43] into the energy function.

Apart from these rather specific problems, several research directions are open. One of them concerns the design of an unifying energy framework that would allow segmentation and tracking of multiple objects, while precluding the incorrect merging of similar objects getting close to each other in the image plane. Another direction of research concerns the automatic tuning of the parameters, which remains an open problem in the recent literature on image labeling (e.g., figure/ground segmentation) with graph cuts.

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We are particularly interested in contributions, which elucidate the relationship between structure or dynamics of biological networks and biological function. This relationship may be observed on different scales, for example, on a global scale, or on the level of subnetworks or motifs.

Several levels exist on which to relate biological function to network structure. Given molecular biological interactions, networks may be analysed with respect to their structural and dynamical patterns, which are associated with phenotypes of interest. On the other hand, experimental profiles (e.g., time series, disturbances) can be used to reverse engineer network structures based on a model of the underlying functional network.

Is it possible to detect the interesting features with the current methods? And how is our picture of the relationship between network structure and biological function affected by the choice of methods?

Perspectives both from simulation approaches as well as the evaluation of experimental data and combinations thereof are welcome and will be integrated within this special issue.

Authors should follow the EURASIP Journal on Bioinformatics and Systems Biology manuscript format described at the journal site <http://www.hindawi.com/journals/bsb/>. Prospective authors should submit an electronic copy of their complete manuscript through the journal Manuscript Tracking System at <http://mts.hindawi.com/>, according to the following timetable:

Manuscript Due	June 1, 2008
First Round of Reviews	September 1, 2008
Publication Date	December 1, 2008

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Special Issue on Signal Processing Advances in Robots and Autonomy

Call for Papers

The capabilities of robots and autonomous systems have increased dramatically over the past years. This success story partly depends on advances in signal processing which provide appropriate and efficient analysis of sensor data and enable autonomy. A key element of the transition of signal processing output to its exploitation inside robots and autonomous systems is the way uncertainty is managed: uncertainty originating from insufficient sensor data, uncertainty about effects of future autonomous actions and, in the case of distributed sensors and actuators (like for a team of robots), uncertainty about communication lines. The aim of this special issue is to focus on recent developments that allow passing this transition path successfully, showing either where signal processing is used in robotics and autonomy or where robotics and autonomy had special demands that had not been fulfilled by signal processing before.

Topics of interest include, but are not limited to:

- Autonomous navigation:
 - Outdoor navigation using geo-information and dedicated indoor navigation solutions
 - Collision avoidance/sense and avoid
 - Dynamic feature maps, and simultaneous localization and mapping (SLAM)
- Path planning:
 - Proactive, based on open-loop optimization
 - Reactive, based on adaptive control or model predictive control (MPC)
 - Probabilistic approaches for maximizing the expected future information
- Exploration:
 - Networked teams of robots
 - Sensor networks which mix static sensors with autonomous moving ones
 - Distributed algorithms and communication aspects

The special issue will focus on the one hand on the development and comparison of algorithmic approaches and on the other hand on their currently ever-widening range of applications in any platform: underwater, surface, ground, and airborne. Special interest lies in probabilistic approaches and setups of distributed sensors and actuators.

Authors should follow the EURASIP Journal on Advances in Signal Processing manuscript format described at <http://www.hindawi.com/journals/asp/>. Prospective authors should submit an electronic copy of their complete manuscript through the journal Manuscript Tracking System at <http://mts.hindawi.com/>, according to the following timetable:

Manuscript Due	August 1, 2008
First Round of Reviews	November 1, 2008
Publication Date	February 1, 2009

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Special Issue on Applications of Signal Processing Techniques to Bioinformatics, Genomics, and Proteomics

Call for Papers

The recent development of high-throughput molecular genetics technologies has brought a major impact to bioinformatics, genomics, and proteomics. Classical signal processing techniques have found powerful applications in extracting and modeling the information provided by genomic and proteomic data. This special issue calls for contributions to modeling and processing of data arising in bioinformatics, genomics, and proteomics using signal processing techniques. Submissions are expected to address theoretical developments, computational aspects, or specific applications. However, all successful submissions are required to be technically solid and provide a good integration of theory with practical data.

Suitable topics for this special issue include but are not limited to:

- Time-frequency representations
- Spectral analysis
- Estimation and detection
- Stochastic modeling of gene regulatory networks
- Signal processing for microarray analysis
- Denoising of genomic data
- Data compression
- Pattern recognition
- Signal processing methods in sequence analysis
- Signal processing for proteomics

Authors should follow the EURASIP Journal on Bioinformatics and Systems Biology manuscript format described at the journal site <http://www.hindawi.com/journals/bsb/>. Prospective authors should submit an electronic copy of their complete manuscript through the EURASIP Journal on Bioinformatics and Systems Biology's Manuscript Tracking System at <http://mts.hindawi.com/>, according to the following timetable:

Manuscript Due	August 1, 2008
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Special Issue on Social Image and Video Content Analysis

Call for Papers

The performance of image and video analysis algorithms for content understanding has improved considerably over the last decade and their practical applications are already appearing in large-scale professional multimedia databases. However, the emergence and growing popularity of social networks and Web 2.0 applications, coupled with the ubiquity of affordable media capture, has recently stimulated huge growth in the amount of personal content available. This content brings very different challenges compared to professionally authored content: it is unstructured (i.e., it needs not conform to a generally accepted high-level syntax), typically complementary sources are available when it is captured or published, and it features the "user-in-the-loop" at all stages of the content life-cycle (capture, editing, publishing, and sharing). To date, user provided metadata, tagging, rating and so on are typically used to index content in such environments. Automated analysis has not been widely deployed yet, as research is needed to adapt existing approaches to address these new challenges.

Research directions such as multimodal fusion, collaborative computing, using location or acquisition metadata, personal and social context, tags, and other contextual information, are currently being explored in such environments. As the Web has become a massive source of multimedia content, the research community responded by developing automated methods that collect and organize ground truth collections of content, vocabularies, and so on, and similar initiatives are now required for social content. The challenge will be to demonstrate that such methods can provide a more powerful experience for the user, generate awareness, and pave the way for innovative future applications.

This issue calls for high quality, original contributions focusing on image and video analysis in large scale, distributed, social networking, and web environments. We particularly welcome papers that explore information fusion, collaborative techniques, or context analysis.

Topics of interest include, but are not limited to:

- Image and video analysis using acquisition, location, and contextual metadata
- Using collection contextual cues to constrain segmentation and classification
- Fusion of textual, audio, and numeric data in visual content analysis

- Knowledge-driven analysis and reasoning in social network environments
- Classification, structuring, and abstraction of large-scale, heterogeneous visual content
- Multimodal person detection and behavior analysis for individuals and groups
- Collaborative visual content annotation and ground truth generation using analysis tools
- User profile modeling in social network environments and personalized visual search
- Visual content analysis employing social interaction and community behavior models
- Using folksonomies, tagging, and social navigation for visual analysis

Authors should follow the EURASIP Journal on Image and Video Processing manuscript format described at <http://www.hindawi.com/journals/ivp/>. Prospective authors should submit an electronic copy of their complete manuscripts through the journal Manuscript Tracking System at <http://mts.hindawi.com/>, according to the following timetable:

Manuscript Due	June 1, 2008
First Round of Reviews	September 1, 2008
Publication Date	December 1, 2008

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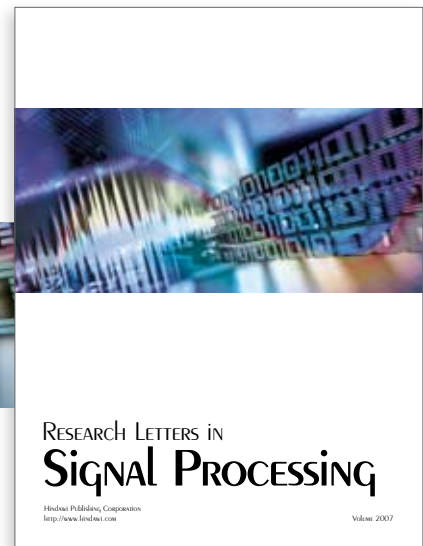
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ISSN: 1687-6911; e-ISSN: 1687-692X; doi:10.1155/RLSP



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