



# Digital image processing

**Aline Roumy**

Inria, Rennes, team Sirocco

# The course: you and me!

- Who am I? Researcher at Inria, Rennes.

Research topic:

communication of visual data (image and video)

Research areas:

image processing and signal processing,  
information theory.

- Who are you?

# Course organization

- introduction to image processing: 3 lectures of 1:10 each
- When **Quiz** in the slides, answer on Socrative  
<https://b.socrative.com/login/student/>  
Room Name: ALINER  
No need to give your true name (no marks for the answer)
- 2 **computer lab** sessions: 3:30 each in matlab
  - ▶ general exercises on image processing (seen in the course)
  - ▶ one project
- **evaluation**: during the computer lab session(s). You will get marks for the two sessions + multiple choice questions test.

## Part 1 - General introduction

What is image processing?

## ...a part of Computer Vision (*vision par ordinateur*)

- **What it is?**

Technology to design machines that can see.

- **First level:** vision

acquisition of an image thanks to a chain that contains optical devices and sensors

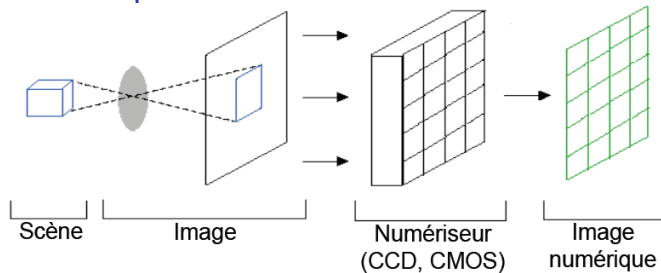
- **Second level: image processing**

modify the image in order to highlight some elements of interest (objects, edges)

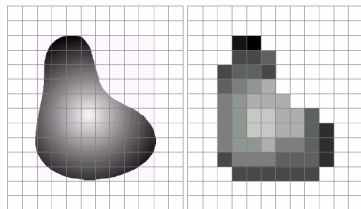
- **Third level:** interpretation, decision making  
use artificial intelligence (AI) to do

- ▶ pattern recognition (*reconnaissance*): identify some shapes in the image (face, coin, ...)
- ▶ image restoration (noise removal, object removal...)
- ▶ 3D scene reconstruction

# First level: acquisition



digitalize = sample (finite number of points)  
+ quantize (finite number of possible gray levels)



## Second level: image processing

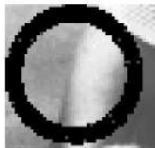
Detect “simple” elements of an image



Une zone homogène



Une texture



Un contour

# Computer vision: a way to extend human perception?

- **Yes!**
  - ▶ because the human visual system is limited
    - in frequencies (wavelength),
    - in angle,
    - in acquisition frequencies (number of images per second):  
high speed camera (camera haute cadence) with thousands images per second...
- **and No!** Computer vision systems are still limited...
  - a machine is **less intelligent** than our brain... but the battle keeps going: (Google's AI Wins Against Go Genius, March 2016)
  - **limited computational capacity** of a machine vs our brain
  - we **use much more information** (not only vision) to make decision



# Application of Computer Vision (vision par ordinateur): Machine Vision (vision industrielle)



- **Use:**  
automatic inspection, (quality inspection)  
process control,  
and robot guidance
- **Works well because...**  
camera designed for a **specific** task  
**controlled** environment

# Application of Computer Vision (vision par ordinateur): natural images

Very challenging (still under research) because **Uncontrolled** environment:

- Acquire an image  
Correct color balance,  
Reconstruct image from projections
- Prepare for display or printing  
Adjust image size, Color mapping
- Facilitate picture storage and transmission  
Efficiently store an image in a digital camera,  
Send an image from mobile
- Enhance and restore images  
Touch up personal photos
- Extract information from images  
Read 2-d bar codes, Character recognition
- Many more ... image processing is ubiquitous



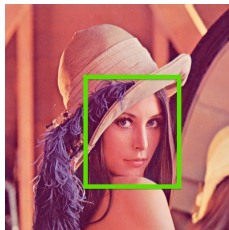
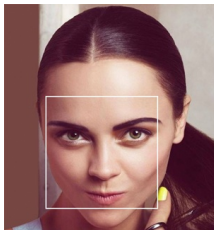
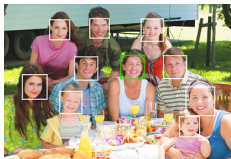
4YCH428

4YCH428

4YCH428

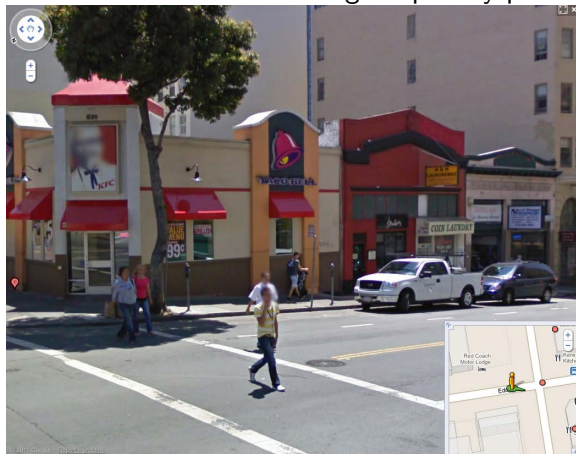
# Application

## Face detection



# Application

## Face blurring for privacy protection



# Application

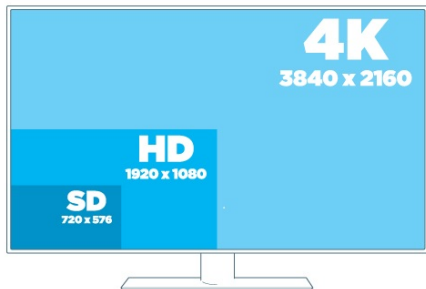
## Object removal (Movie production)



# Application

## Super Resolution a.k.a. Upscaling

Seiki's U-Vision Upscaling HDMI Cable (CES 14)



input

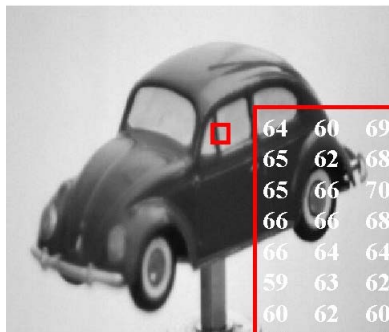


upsizing



super-resolution

## What is an image?

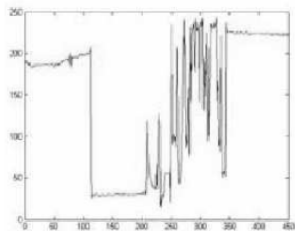


64	60	69	100	149	151	176	182	179
65	62	68	97	145	148	175	183	181
65	66	70	95	142	146	176	185	184
66	66	68	90	135	140	172	184	184
66	64	64	84	129	134	168	181	182
59	63	62	88	130	128	166	185	180
60	62	60	85	127	125	163	183	178
62	62	58	81	122	120	160	181	176
63	64	58	78	118	117	159	180	176

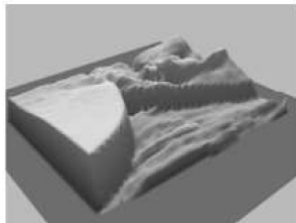
- **Digital image:** 2D array  $I[x, y]$
- Each element is called a **pixel** or pel (from “picture element”)
- Gray levels - 1 byte = 8 bits  $\in [0, 255]$ ,
  - ▶ 0 - black
  - ▶ 255 - white

# What is an image?

a row of an image: is a curve



the whole image: a surface





## Images as matrices

- **Digital image:** is a 2D array (or **matrix**) with  $Nrows$  rows and  $Ncolumns$  columns with elements  $I[i,j] \in \{0, \dots, 255\}$

TP In MATLAB, an image is a matrix "I" with elements  $I(i,j) \in \{0, \dots, 255\}$ : **() NOT [ ]**  
for  $i = 1, \dots, Nrows$ ,  $j = 1, \dots, Ncolumns$ .

TP In Matlab,  $I(:, i)$  denotes the  $i$ -th column of I.

TP **Warning:** type of the 2D array (uint8 or double)

To display an image stored as uint8 `imshow(I)`

To display an image stored as double `imshow(I/255)`

Look at the type of your matrix in the Matlab's **workspace** window → see *Matlab*

# What is an image?

Reading and displaying order of  $I[x, y]$  is:

as a matrix, not as the cartesian coordinate plane

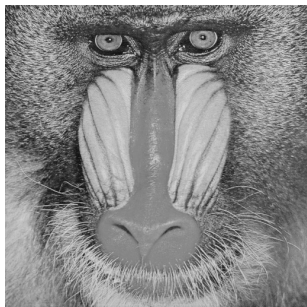
$x$  = row index /  $y$  = column index

BUT the definition is Nb\_columns  $\times$  Nb\_rows (convention)

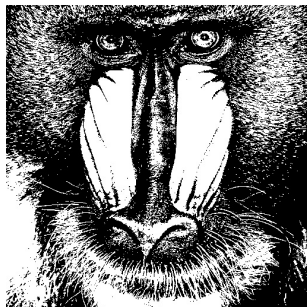
	$y =$									
	58	59	60	61	62	63	64	65	66	67
$x =$ 41	210	209	204	202	197	247	143	71	64	80
42	206	196	203	197	195	210	207	56	63	58
43	201	207	192	201	198	213	156	69	65	57
44	216	206	211	193	202	207	208	57	69	60
45	221	206	211	194	196	197	220	56	63	60
46	209	214	224	199	194	193	204	173	64	60
47	204	212	213	208	191	190	191	214	60	62
48	214	215	215	207	208	180	172	188	69	72
49	209	205	214	205	204	196	187	196	86	62
50	208	209	205	203	202	186	174	185	149	71
51	207	210	211	199	217	194	183	177	209	90
52	208	205	209	209	197	194	183	187	187	239
53	204	206	203	209	195	203	188	185	183	221
54	200	203	199	236	188	197	183	190	183	196
55	205	210	202	203	199	197	196	181	173	186



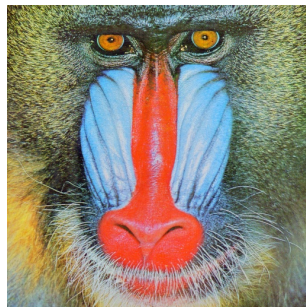
## Some types of images



Gray level image  
 $I[x, y] \in [0, 255]$



Gray level image  
 $I[x, y] \in \{0, 1\}$

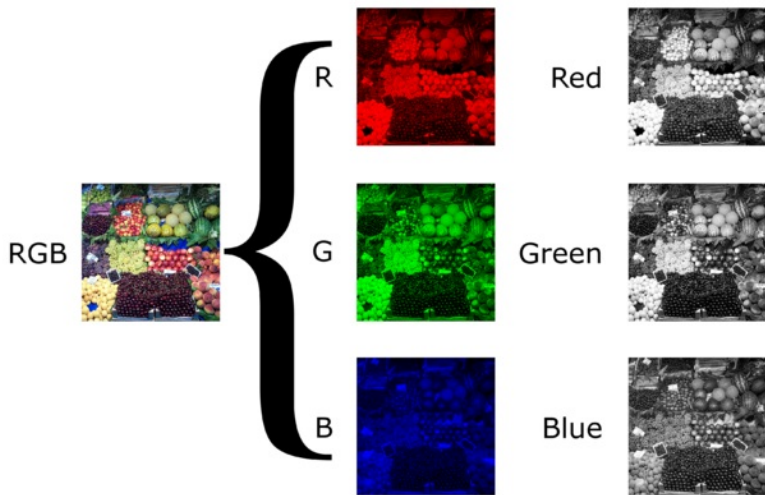


Color image  
 $I_R[x, y] I_G[x, y] I_B[x, y]$

and many more types (3D, High Dynamic Range (HDR)...)

**Quiz 1,2,3**

# Color Components



but there exists [other representations](#) for color images (Luminance Chrominance)

# Outline of the course

Part 1 - General introduction

Part 2 - Image transformation

3 kinds of transformation

Part 3 - Point-to-point transformation

Geometric transformation

Contrast enhancement/reduction

Gray level histograms

Quantization, binarization

Part 4 - Local to point transformation

Morphological image processing

Image filtering, convolution

LOW pass filtering

HIGH pass filtering

Downsampling and Interpolation/Upsampling

Segmentation

Part 5 - Global to point transformation

Part 6 - Quality measure

Part 7 - Machine learning

## Part 2 - Image transformation

How to formalize an image transformation such that it can be **automatically processed** by a computer?

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# Image transformation

What is an image?

- from the **mathematical** perspective:
  - ▶ an image is a matrix
  - ▶ many tools exist to manipulate matrices
- from the **human** perspective:
  - ▶ an image contains **semantic** information
  - ▶ need to interpret the image beyond the luminance values

Transformation:  $T$

$$T : [0, 255]^{Nrows \times Ncolumns} \rightarrow [0, 255]^{Nrows' \times Ncolumns'}$$

$$im[x, y] \mapsto IM[u, v]$$

- $im$  = input or original image
- $IM$  = transformed image
- $x, y$  and  $u, v$  are the spatial coordinates of a pixel

**Goal of a transformation:**

get a **a new representation** of the input picture  
to ease the extraction of particular properties of the picture.

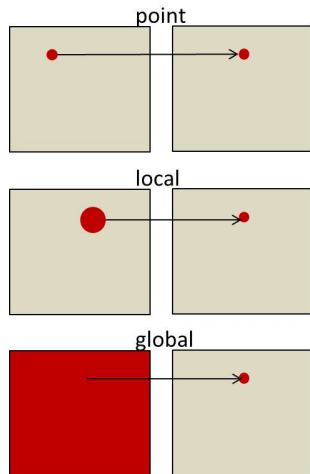


## 3 kinds of transformation

There exist 3 types of transformation:

- Point to point transformation: The output value at a specific coordinate depends **only** on one input value but **not necessarily at the same coordinate**;
- Local to point transformation: The output value at a specific coordinate depends on the input values in the **neighborhood** of that same coordinate;
- Global to point transformation: The output value at a specific coordinate depends on **all** the values in the input image.

Note that the complexity increases with the size of the considered neighborhood...



## Part 3 - Point-to-point transformation

When a pixel of the new (transformed) image **only** depends on a **single** pixel of the input image

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# Geometric transformation

- Geometric transformation such as rotation, scaling...
- Examples:



original



a.

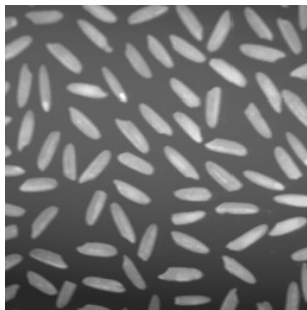


b.

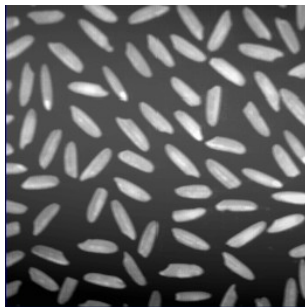
**Quiz 4,5,6**

# Contrast enhancement/reduction

Images with different contrast



low contrast



high contrast

## Contrast definition

Many definitions for the contrast for a  $N \times M$  image  $f[x, y]$ :

- **standard deviation** (average variation) of the Gray levels

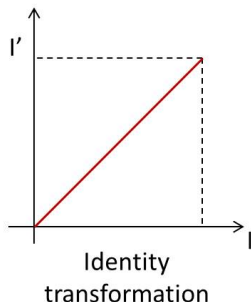
$$C = \sqrt{\frac{1}{N M} \sum_{x=1}^N \sum_{y=1}^M (f[x, y] - \text{mean})^2}$$

- **variation between the minimum and the maximum** of the Gray levels

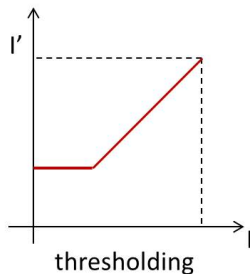
$$C = \frac{\max_{x,y} (f[x, y]) - \min_{x,y} (f[x, y])}{\max_{x,y} (f[x, y]) + \min_{x,y} (f[x, y])}$$

# Functions applied to the luminance

- $I$ : input luminance value

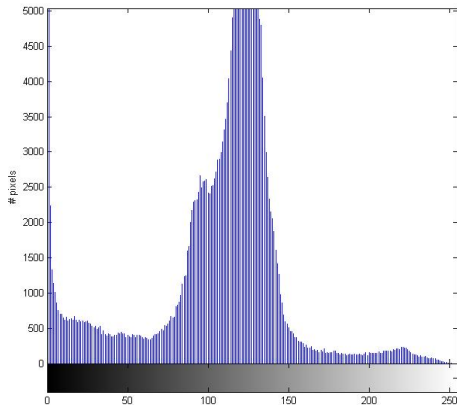


- $I'$ : output luminance value



**Quiz 7**

# Gray level histograms



*zebra image*

- the histogram represents the “distribution” of the gray level in an image
- $H(k) = \# \text{pixels having gray level } k$ .



# Gray level histograms

- To measure a histogram:
  - ▶ For B-bit image, initialize  $2^B$  counters with 0
  - ▶ Loop over all pixels  $x, y$
  - ▶ When encountering gray level  $f[x, y] = i$ , increment counter  $\#i$
- Normalized histogram can be thought of as an estimate of the probability distribution (pdf) of the continuous signal amplitude
- Use fewer, larger bins to trade off amplitude resolution against sample size.

**Quiz 8, 9, 10**

## Histogram adjustment... with linear transform

**Goal:** **Augment** the contrast (i.e. augment the difference between two displayed gray levels).

**Idea:** Find an **affine** transformation

$$g = F(f)$$

that is applied to each pixel of the input image  $f[x, y]$ , such that the distribution of gray levels for the output image  $g[x, y]$  **spans the whole range**  $[0, 255]$ .

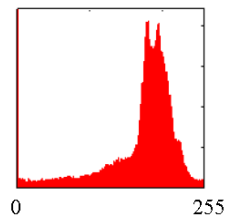
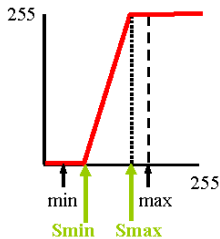
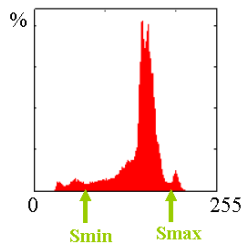
$$\begin{aligned} F : [min, max] &\rightarrow [0, 255] \\ x &\mapsto F(x) = ax + b \end{aligned}$$

where  $x$  stands for the gray level.

i.e. **find  $a$  and  $b$** .

**Quiz 11**

# Histogram adjustment... with linear transform and saturation



# Histogram equalization

**Idea:** Find a **non-linear** transformation

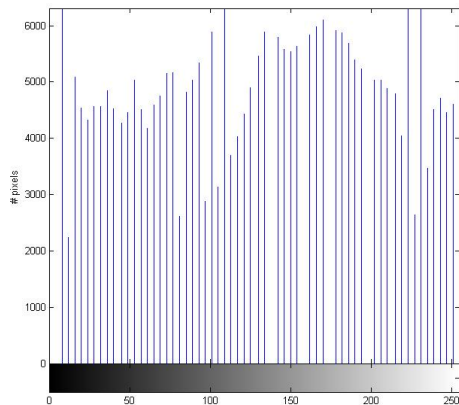
$$g = T(f)$$

that is applied to each pixel of the input image  $f[x, y]$ , such that a uniform distribution of gray levels results for the output image  $g[x, y]$ .

Use the cumulative distribution function (cdf) (*Fonction de répartition*).

## Quiz 12

# Histogram equalization example

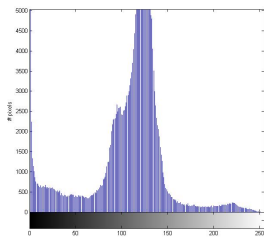


*zebra image*

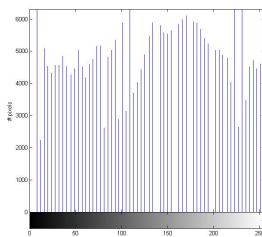
#pixels vs gray level

# Histogram equalization example

Original image zebra ...



after histogram equalization



## Quantization... if time permits

The quantization is a process to represent a large set of values with a smaller set.

**Scalar** quantization:

$$\begin{aligned} Q : \mathcal{X} &\rightarrow \mathcal{C} = \{y_i\}_{i=1,2,\dots,N} \\ x &\mapsto Q(x) \end{aligned}$$

- $N$  is the number of quantization level;
- $\mathcal{X}$  can be continuous (ex:  $\mathbb{R}$ ) or discrete;
- $\mathcal{C}$  is always discrete (codebook, dictionary);
- if  $\mathcal{X}$  discrete,  $\text{card}(\mathcal{X}) > \text{card}(\mathcal{C})$ ;
- Since  $\text{card}(\mathcal{X}) > \text{card}(\mathcal{C})$ ,  $Q$  is non injective, we loose some information (**lossy compression**).

### Quiz 13

# Uniform scalar Quantization (if time permits)

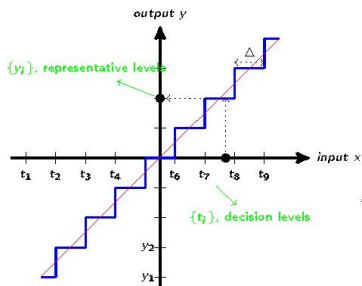
In uniform scalar quantization, the quantization step size is fixed, no matter the signal amplitude is.

Definition:

- The quantization thresholds are uniformly spread:  
 $\forall i \in \{1, \dots, N\}, t_{i+1} - t_i = \Delta$
- The output values are the centers of the quantization interval:  
 $\forall i \in \{1, \dots, N\}, y_i = \frac{t_{i+1} + t_i}{2}$

Implementation:

$$Q(x) = \Delta \times \left\lfloor \frac{x}{\Delta} + 0.5 \right\rfloor$$





# Uniform scalar Quantization

Application to images:



quality resolution (résolution tonale)

**Quiz 14 15**

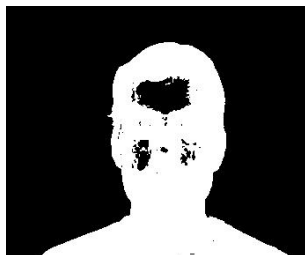
## Binarization: by Gray-level thresholding



Original image  
Peter  $f[x, y]$



**Thresholded**  
Peter  $t[x, y]$



**Mask**  
 $1 - t[x, y]$

**Thresholding:** Loop over all pixels  $x, y$

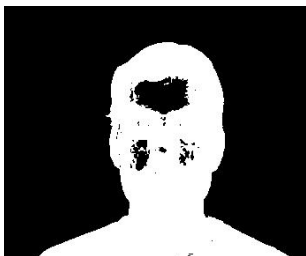
- if  $f[x, y] > \text{threshold}$ ,  $t[x, y] = 1$
- else  $t[x, y] = 0$ .

**Mask:** logical image  
region of interest=1  
rest=0

## Binarization: to extract foreground



Original image  
Peter  $f[x, y]$



**Mask**  
 $1 - t[x, y]$



Peter **foreground**  
 $f[x, y].(1 - t[x, y])$

**Thresholding:** Loop over all pixels  $x, y$

- if  $f[x, y] > \text{threshold}$ ,  $t[x, y] = 1$
- else  $t[x, y] = 0$ .

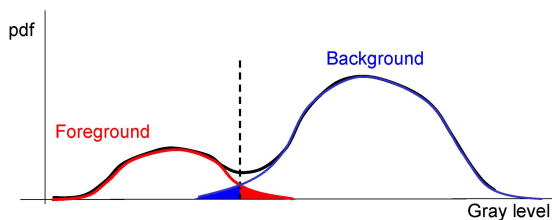
**Mask:** logical image  
region of interest=1  
rest=0

$f.*\text{mask}=\text{foreground}$

**Question:** How can holes be filled?

# How can holes be filled?

## 1. By **adjusting the threshold**



There exists automatic threshold determination.  
In TP, we will do it manually.

- ## 2. Decision based on a single pixel is **not sufficient** need decision based on **neighborhood**: **local to point** transformation

## Part 4 - Local to point transformation

When a pixel of the new (transformed) image depends on a **limited** set of pixels of the input image

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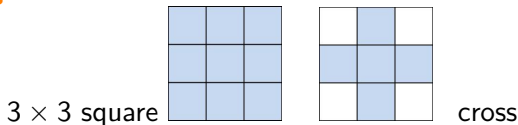
Part 7 - Machine learning

# Morphological image processing for **binary** images

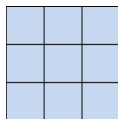
- Binary images are common
  - ▶ Source image is binary:  
Text, line graphics
  - ▶ Features extracted from a gray-scale/color image
    - Edges;
    - Presence/absence of some object in the image
- Representation of individual pixels as 0 or 1, convention:  
object (foreground) = 1 (white)  
background = 0 (black)
- Morphological image processing has been generalized to gray-level images via level sets

# Structuring element

- **Structuring element = a mask**



- **For each pixel**  $(i, j)$ , apply the mask/structuring element centered in  $(i, j)$



mask

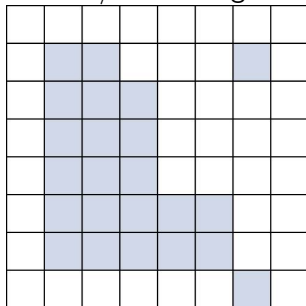


image 8x8

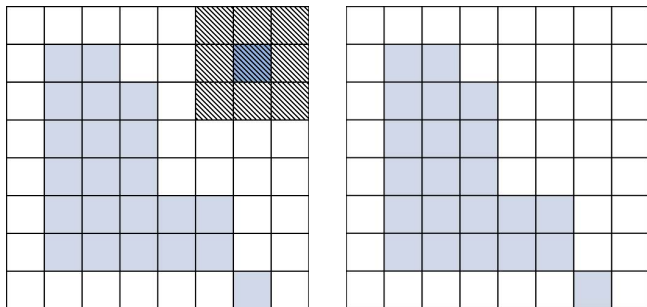
For ease of visualization (unlike convention):

background 0 black  $\rightarrow$  white / object 1 white  $\rightarrow$  blue



# Erosion

**Erosion** if **one** pixel under the mask belongs to the **background** (white), then the **centered** pixel becomes **background** (white)  
i.e. *erosion of the object*



- Erosion of the object!

# Erosion

## Quiz 16

Which a or b is the eroded image? The mask is

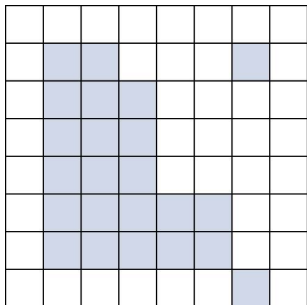
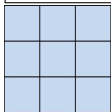
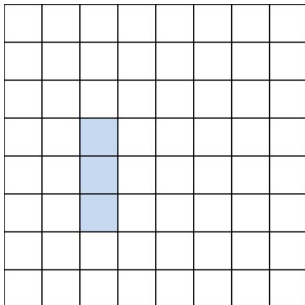
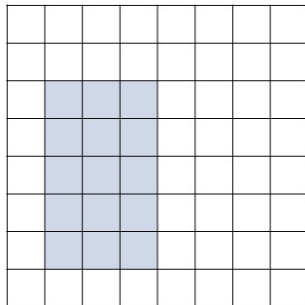


image 8x8



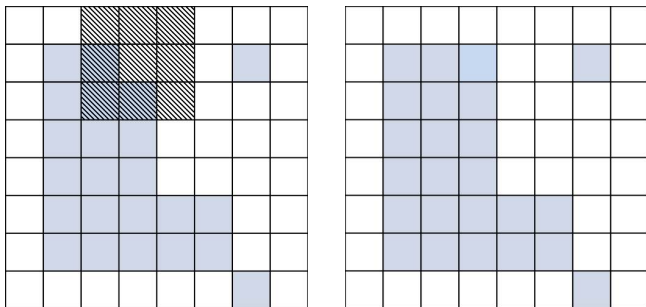
a. eroded image?



b. eroded image?

# Dilation

**Dilation** if **one** pixel under the mask belongs to the **object** (blue), then the **centered** pixel becomes **object**



- Dilation **of the object!**
- Duality: erosion is dilation of the background

# Dilation

## Quiz 17

Which (a or b) is the dilated image? The mask is

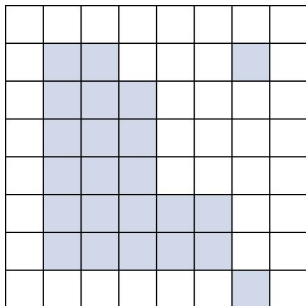
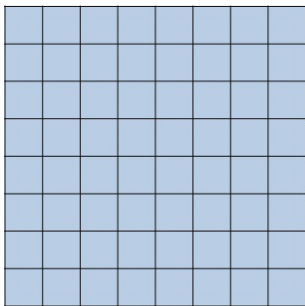
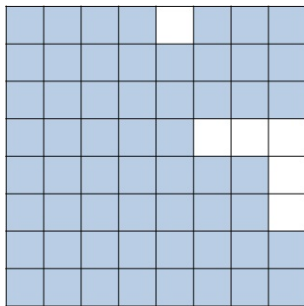


image 8x8

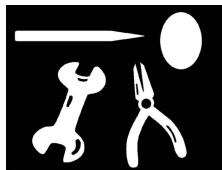


a. dilated image?

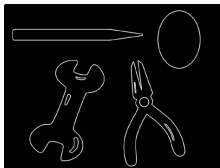


b. dilated image?

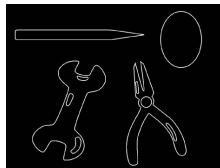
## Application: Morphological edge detectors



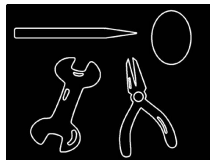
$f[x,y]$   
object



$\text{dilate}(f)-f$   
a.



$f-\text{erode}(f)$   
b.



$\text{dilate}(f)-\text{erode}(f)$   
c.

**Quiz 18,19, 20**

## Morphological operators

- **Erosion** if one pixel under the mask belongs to the background, then the centered pixel becomes background  
i.e. *erosion of the object*
- **Dilation** if one pixel under the mask belongs to the object, then the centered pixel becomes object  
i.e. *dilation of the object*
- **Opening** erosion and then dilation  
GOAL: remove noise (small elements)
- **Closing** dilation and then erosion  
GOAL: fill in holes in the object or make connex 2 objects that were separated due to noise

## Application: Denoising



$f[x,y]$



binarized

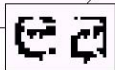


opening

Source: Gonzalez and Woods. Digital Image Processing.

# Application: Recognition with closing

Historically, certain computer programs were written using only two digits rather than four to define the applicable year. Accordingly, the company's software may recognize a date using "00" as 1900 rather than the year 2000.



**Historically, certain computer programs were written using only two digits rather than four to define the applicable year. Accordingly, the company's software may recognize a date using "00" as 1900 rather than the year 2000.**



0	1	0
1	1	1
0	1	0

a c  
b

**FIGURE 9.5**

(a) Sample text of poor resolution with broken characters (magnified view). (b) Structuring element. (c) Dilation of (a) by (b). Broken segments were joined.

Source: Gonzalez and Woods. Digital Image Processing.



Part 1 - General introduction

Part 2 - Image transformation

3 kinds of transformation

Part 3 - Point-to-point transformation

Geometric transformation

Contrast enhancement/reduction

Gray level histograms

Quantization, binarization

Part 4 - Local to point transformation

Morphological image processing

Image filtering, convolution

LOW pass filtering

HIGH pass filtering

Downsampling and Interpolation/Upsampling

Segmentation

Part 5 - Global to point transformation

Part 6 - Quality measure

Part 7 - Machine learning

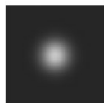
# Filtering

- **Filtering** is a **local to point** transformation: the new pixel value depends on the current but also neighboring pixels
- For each pixel, we **apply a mask**.
- If the filter is **linear**, then, for each applied mask, the centered pixel becomes a **linear** (more precisely convex) **combination** of the pixel values in the mask.



input image

\*

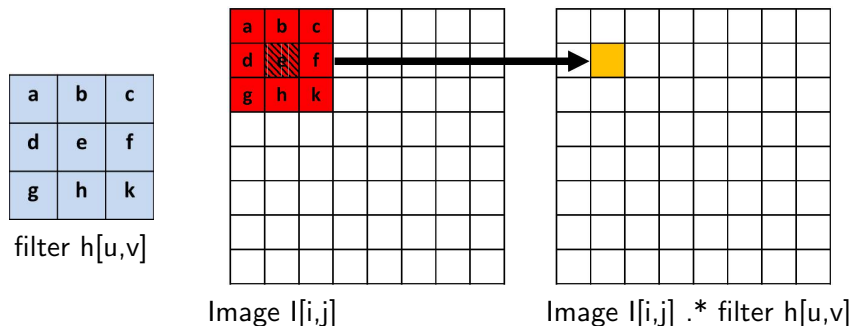


=



output image

## Image filtering: the steps



$J$  is the output of filtering of  $I$  by  $h$ :

$$\begin{aligned} J[2, 2] = & a \times I[1, 1] + b \times I[1, 2] + c \times I[1, 3] \\ & + d \times I[2, 1] + e \times I[2, 2] + f \times I[2, 3] \\ & + g \times I[3, 1] + h \times I[3, 2] + k \times I[3, 3] \end{aligned}$$

## Image filtering: the steps

a	b	c
d	e	f
g	h	k

filter  $h[u,v]$

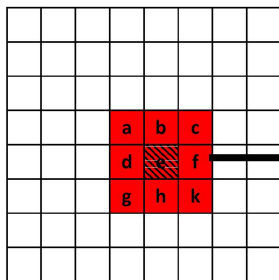


Image  $I[i,j]$

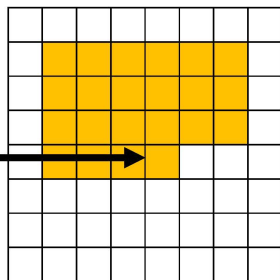


Image  $I[i,j] \cdot * \text{filter } h[u,v]$

$$\begin{aligned} J[i,j] = & a \times I[i-1,j-1] + b \times I[i-1,j] + c \times I[i-1,j+1] \\ & + d \times I[i,j-1] + e \times I[i,j] + f \times I[i,j+1] \\ & + g \times I[i+1,j-1] + h \times I[i+1,j] + k \times I[i+1,j+1] \end{aligned}$$

## Filtering: the equations

- A compact way to write the equations of 2D linear filtering is: 2D discrete convolution.
- Reminder: 1D discrete convolution

$$g[x] = f[x] * h[x] = \sum_k h[x - k] f[k] = \sum_k h[k] f[x - k]$$

- ▶ f: input
  - ▶ g: output
  - ▶ h: filter, convolution kernel
- a **linear** filter: is the convolution of  $f$  by the filter  $h$  i.e. it is the **linear combination** of the neighboring pixel values

## Image filtering: the equations

$$\begin{aligned} J[x, y] &= I[x, y] * h[x, y] = \sum_{u, v} h[x - u, y - v] I[u, v] \\ &= \sum_{u, v \in \{-1, 0, 1\}^2} h[u, v] I[x - u, y - v] \end{aligned}$$

**Example:** Gaussian filter



$I[x, y]$



$J[x, y]$

# Image filtering: border effect and normalization

Border effect: solutions:

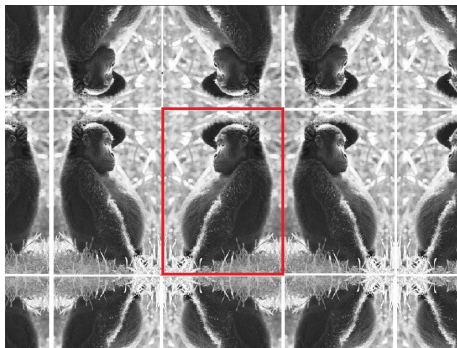
- Set the borders of  $J$  to 0
- Convolution of part of the mask, where  $I$  exists

?	?	?	?	?	?	?	?
?							?
?							?
?							?
?							?
?							?
?							?
?	?	?	?	?	?	?	?

- mirror of the image  $I[i, j]$

## Normalization:

to visualize the filtered image, one needs to **normalize** the output by dividing by the sum of the filter coefficients.



# Filtering what? some frequency components in the image

- What is a **frequency in an image**?

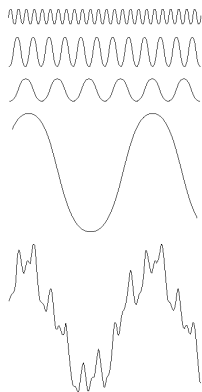
To answer the question:

- What is a **frequency in a signal**?

**high** frequencies

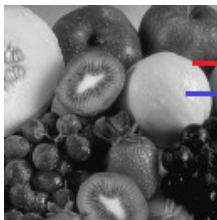
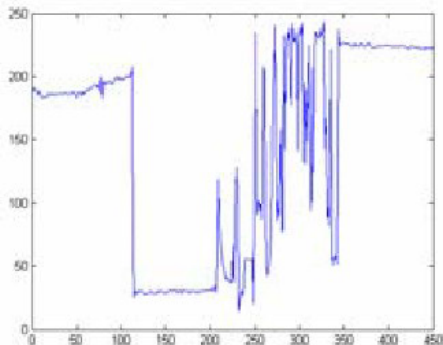
**low** frequency

sum of all 4 frequencies





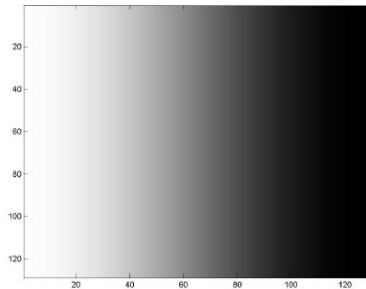
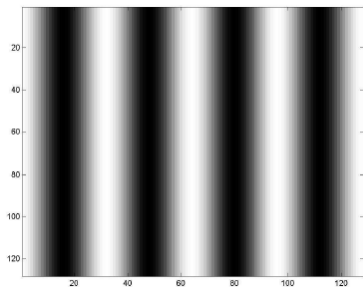
## What is a frequency... in the image



high  
low

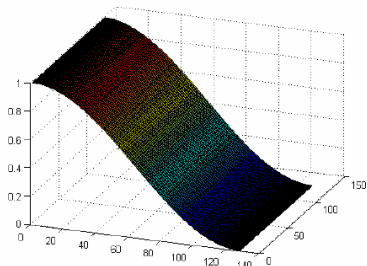
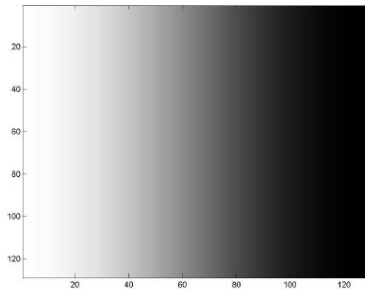
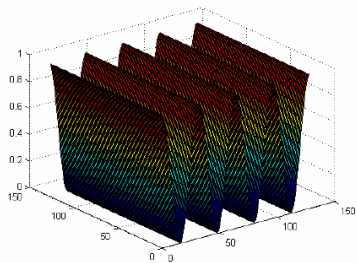
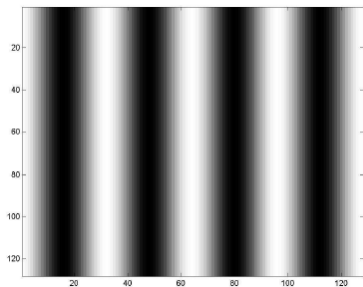
- low frequency: smooth areas
- high frequency: abrupt changes in the luminance

# What is a frequency... in the image



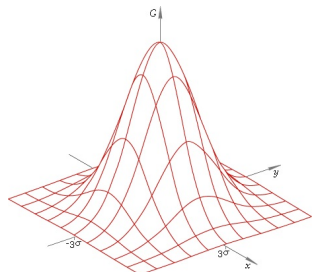
low/ high frequency?

# What is a frequency... in the image



# LOW pass filtering

- Mean filter
- Gaussian



$$G(x, y) = \frac{1}{2\pi\sigma^2} e^{-\frac{x^2+y^2}{2\sigma^2}}$$

1/9	1/9	1/9
1/9	1/9	1/9
1/9	1/9	1/9

$$\frac{1}{273}$$

1	4	7	4	1
4	16	26	16	4
7	26	41	26	7
4	16	26	16	4
1	4	7	4	1

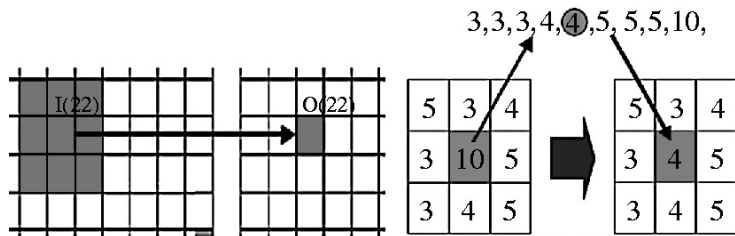
discrete  $G(x, y)$   $\sigma = 1$

Discretized approximation to  $G(x, y)$ :

- by averaging over a pixel area (0.001 precision)
- fspecial in Matlab uses the value of the Gaussian at the centre of a pixel in the mask.

# LOW pass filtering

- Median



**Quiz 21 to 24**

## LOW pass filtering: results



original image



5 x 5 mean filter



5 x 5 Gaussian filter



5 x 5 median filter

## LOW pass filtering: results

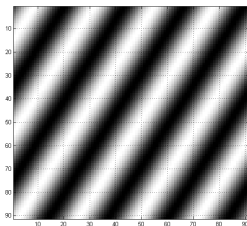
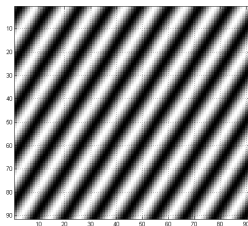
### Quiz 25, 26

25 Is it true?

LP filtering keeps low frequencies of an image.

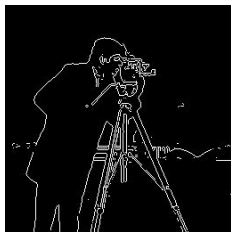
26 Is it true?

image a (below) contains higher frequencies than image b.



## Image filtering: type of filters

- **LOW** pass filter:  
eliminate high frequencies.  
Application: smoothing,  
blurring, erasing noise...



- **HIGH** pass filter:  
eliminate low frequencies.  
Application:  
edge detection, enhance  
details...



# HIGH pass filtering

## Properties:

- Edge (contour): corresponds to abrupt changes in the lumimance i.e. high frequencies
- i.e. HP filters exhibit regions with high gradient of the gray level values

**Quiz 27**

# Edge detection in 1D

Image 1D  $f(x)$



1ère dérivée  $f'(x)$



$|f'(x)|$



**Pixels contours:**  
 $|f'(x)| > \text{Seuil}$



- Edges corresponds to the extrema of the norm of the 1st derivative or equivalently to the zeros of the 2nd derivative.

# HIGH pass filtering

2D derivation operators: gradient, laplacian...

- 1st derivative: Gradient

$$\nabla f|_{x_0, y_0} = \frac{\partial f}{\partial x}(x_0, y_0)\mathbf{e}_x + \frac{\partial f}{\partial y}(x_0, y_0)\mathbf{e}_y,$$
$$\text{norm } |\nabla f|^2 = \left(\frac{\partial f}{\partial x}\right)^2 + \left(\frac{\partial f}{\partial y}\right)^2$$

- 2nd derivative: Laplacian

$$\nabla^2 f = \frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial y^2}$$

- edges corresponds to the extrema of the norm of the gradient or equivalently to the zeros of the Laplacian.

# Gradient computation

## Discretization of the Gradient

**Quiz 28,29**

$$\frac{\Delta I}{\Delta x} = \frac{I(x + \Delta x) - I(x)}{\Delta x}$$

Let us assume that  $\Delta x = 1$

- vertical axis direction, (detection of horizontal edges) , then  $\Delta I = I[1 + i, j] - I[i, j]$

$$\text{filter: } \begin{pmatrix} -1 \\ 0 \\ 1 \end{pmatrix} \text{ or } \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

- horizontal axis direction, (detection of vertical edges) , then  $\Delta I = I[i, j + 1] - I[i, j]$

$$\text{filter: } (-1, 0, 1) \text{ or } (-1, 1)$$

## HIGH pass filtering (gradient): results



original image



Gradient vertical



Gradient horizontal



Gradient norm

**Quiz 30**

# Other HP filters

**Filtre de Prewitt** : Moyenneur + Dérivée

$$\begin{pmatrix} -1 & 0 & 1 \\ -1 & 0 & 1 \\ -1 & 0 & 1 \end{pmatrix} = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix} * (-1 \ 0 \ 1) \quad \begin{pmatrix} -1 & -1 & -1 \\ 0 & 0 & 0 \\ 1 & 1 & 1 \end{pmatrix} = \begin{pmatrix} -1 \\ 0 \\ 1 \end{pmatrix} * (1 \ 1 \ 1)$$

**Filtre de Sobel** : Gaussienne + Dérivée

$$\begin{pmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{pmatrix} = \begin{pmatrix} 1 \\ 2 \\ 1 \end{pmatrix} * (-1 \ 0 \ 1) \quad \begin{pmatrix} -1 & -2 & -1 \\ 0 & 0 & 0 \\ 1 & 2 & 1 \end{pmatrix} = \begin{pmatrix} -1 \\ 0 \\ 1 \end{pmatrix} * (1 \ 2 \ 1)$$

⇒ *Détection des contours moins sensible au bruit*

Quiz 31, 32



original



Prewitt



Sobel

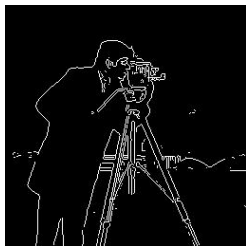
## HIGH pass filtering: results after thresholding



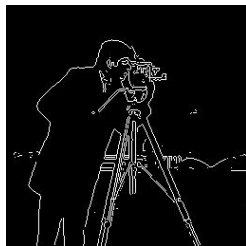
original image



Gradient norm



Prewitt



Sobel

## Edge detection based on Laplacian

- Second derivative of a continuous 2D function  $f = \text{Laplacian}$

$$\nabla^2 f = \frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial y^2}$$

- for a discrete image  $I$ , discretized by

$$\nabla^2 I = I[i+1, j] + I[i-1, j] + I[i, j+1] + I[i, j-1] - 4 I[i, j]$$

$$\begin{pmatrix} 0 & 1 & 0 \\ 1 & -4 & 1 \\ 0 & 1 & 0 \end{pmatrix}$$

- the edges correspond to zero crossing of the Laplacian



# Result of edge detection



original



Sobel



Laplacian

Part 1 - General introduction

Part 2 - Image transformation

3 kinds of transformation

Part 3 - Point-to-point transformation

Geometric transformation

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Quantization, binarization

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LOW pass filtering

HIGH pass filtering

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Part 6 - Quality measure

Part 7 - Machine learning

## Downsampling (if time permits)

**Aliasing:** occurs when downsampling without low pass filtering



Properly sampled image of brick wall.

Spatial aliasing

Downsampling with proper low pass filtering:



256x256



128x128

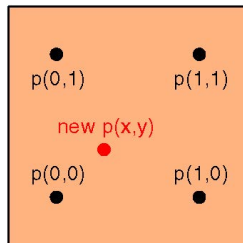


64x64



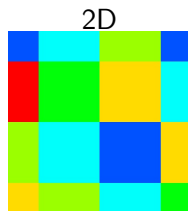
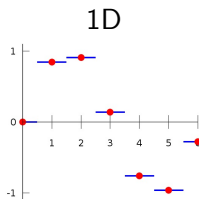
32x32

# Interpolation/Upsampling

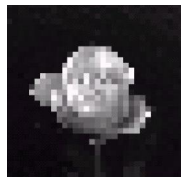


# Interpolation/Upsampling

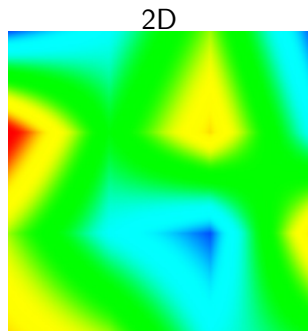
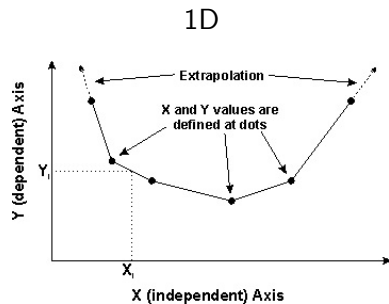
- Nearest Neighbor (NN) method



Drawback: blocking effect



# Bilinear Interpolation

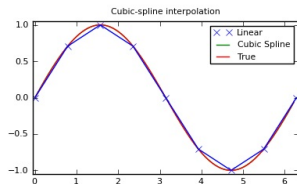


Avoid blocking effect BUT non smooth i.e. non natural

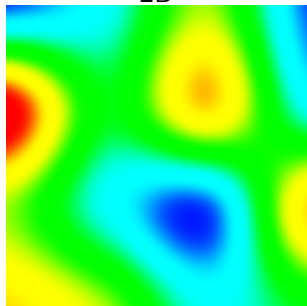
# Bicubic Interpolation

- linear combination of the 16 neighboring pixels. The weights depend on the distance between the neighboring pixel and the pixel to be interpolated
- **bicubic interpolation** achieves a good complexity/rendering tradeoff

1D



2D



# Interpolation: the results



*Plus proche  
voisin*



*Bilinéaire*



a	b	c
d	e	f

**FIGURE 2.25** Top row: images zoomed from  $128 \times 128$ ,  $64 \times 64$ , and  $32 \times 32$  pixels to  $1024 \times 1024$  pixels, using nearest neighbor gray-level interpolation. Bottom row: same sequence, but using bilinear interpolation.



## Interpolation: the results



*Plus proche  
voisin*



*Bilinéaire  
(4  
voisins)*



## Interpolation: the results



*Bilinéaire*  
(4  
voisins)



*Bicubique*  
(16 voisins)



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Part 5 - Global to point transformation

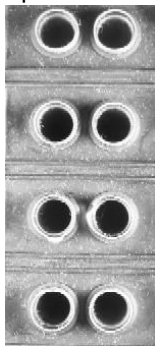
Part 6 - Quality measure

Part 7 - Machine learning

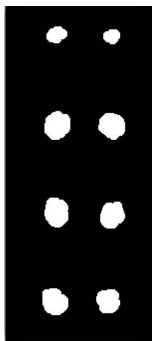
## Image segmentation is...

- the process of **partitioning** a digital image into multiple segments,
- the process of **assigning a label** to every pixel in an image such that pixels with the same label share certain characteristics.

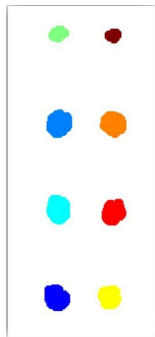
Example: counting holes.



original



detect holes

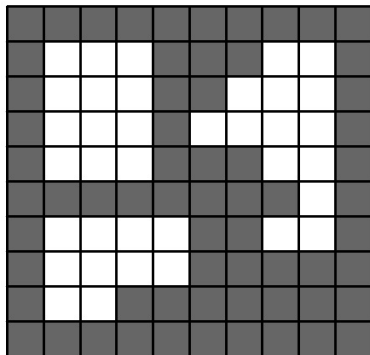


label

# Label connected components in 2-D binary image



- Nous allons effectuer un parcours de l'image pour affecter un numéro unique (étiquette) pour chaque région
- Tous les pixels d'une même région doivent avoir le même numéro (étiquette)



Source: A. Boucher IFI

# first iteration

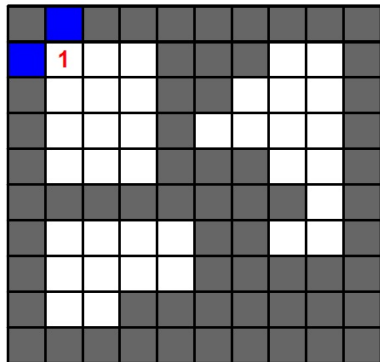
## Premier parcours de l'image

- Pour chaque pixel d'une région, on lui affecte
  - soit la plus petite étiquette parmi ses voisins **haut** et **gauche**
  - soit une nouvelle étiquette.

Parcours



Voisinage



# first iteration

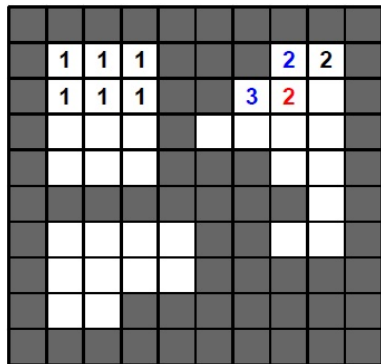
## Premier parcours de l'image

- Pour chaque pixel d'une région, on lui affecte
  - soit la plus petite étiquette parmi ses voisins **haut** et **gauche**
  - soit une nouvelle étiquette.

Parcours



Voisinage



# first iteration

## Premier parcours de l'image

- Pour chaque pixel d'une région, on lui affecte
  - soit la plus petite étiquette parmi ses voisins **haut** et **gauche**
  - soit une nouvelle étiquette.

Parcours



Voisinage



	1	1	1				2	2	
	1	1	1			3	2	2	
	1	1	1		4	3	2	2	
	1	1	1				2	2	
								2	
	5	5	5	5			6	2	
	5	5	5	5					
	5	5							



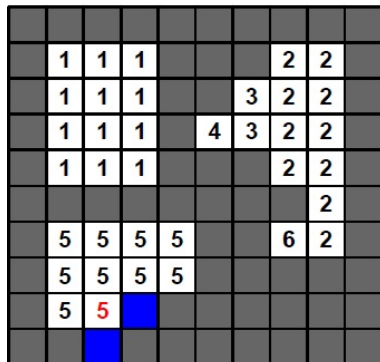
## SECOND iteration

### Deuxième parcours de l'image

- Pour chaque pixel d'une région, on lui affecte
  - la plus petite étiquette parmi la sienne et celles ses voisins bas et droite

Parcours 

Voisinage 



## SECOND iteration

### Deuxième parcours de l'image

- Pour chaque pixel d'une région, on lui affecte
  - la plus petite étiquette parmi la sienne et celles ses voisins bas et droite

Parcours 

Voisinage 

	1	1	1				2	2	
	1	1	1			2	2	2	
	1	1	1		2	2	2	2	
	1	1	1				2	2	
								2	
	5	5	5	5			2	2	
	5	5	5	5					
	5	5							

## Label connected components in 2-D binary image

- in this example, 2 iterations were sufficient to perform segmentation,
- in general, more than 2 iterations are needed,
- the iterations are performed until there is no more change in the labels: so indeed, we should have performed a last iteration to be sure that the labels would no change.

**Quiz 33 to 35**

## Part 5 - Global to point transformation

When a pixel of the new (transformed) image depends on a the  
whole input image

Part 1 - General introduction

Part 2 - Image transformation

3 kinds of transformation

Part 3 - Point-to-point transformation

Geometric transformation

Contrast enhancement/reduction

Gray level histograms

Quantization, binarization

Part 4 - Local to point transformation

Morphological image processing

Image filtering, convolution

LOW pass filtering

HIGH pass filtering

Downsampling and Interpolation/Upsampling

Segmentation

Part 5 - Global to point transformation

Part 6 - Quality measure

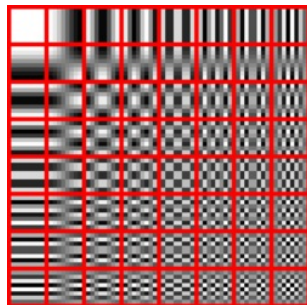
Part 7 - Machine learning

## DCT: Discrete cosine transform

Change of basis:

Decomposition of the input patch  $x_{n_1, n_2}$   
into the coefficients  $X_{k_1, k_2}$  in the new basis

$$X_{k_1, k_2} = \sum_{n_1=0}^{N_1-1} \left( \sum_{n_2=0}^{N_2-1} x_{n_1, n_2} \cos \left[ \frac{\pi}{N_2} \left( n_2 + \frac{1}{2} \right) k_2 \right] \right) \cos \left[ \frac{\pi}{N_1} \left( n_1 + \frac{1}{2} \right) k_1 \right]$$



basis functions of the  
2D-DCT for  $8 \times 8$   
patches

Used in jpeg image compression, and mpeg-2, mpeg-4, hevc video  
compression

**Quiz 36 to 39**

## Part 6 - Quality measure

How to assess that an image transformation **works** correctly?

Part 1 - General introduction

Part 2 - Image transformation

3 kinds of transformation

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**LOW** pass filtering

**HIGH** pass filtering

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Part 5 - Global to point transformation

Part 6 - Quality measure

Part 7 - Machine learning



## An **objective** quality measure

### Peak signal-to-noise ratio (PSNR):

- measures the distortion between two images  $I$  and  $K$
- defined via the mean squared error (MSE):

$$MSE = \frac{1}{m n} \sum_{i=1}^m \sum_{j=1}^n (I[i, j] - K[i, j])^2$$

and

$$PSNR = 10 \cdot \log_{10} \left( \frac{MAX_I^2}{MSE} \right)$$

For instance,  $MAX = 255$ .

- if  $I =$  true image and  $K$  the processed image, PSNR is a quantitative measure of the quality of the image
- The higher the better...

## Part 7 - Machine learning

How to **learn** automatically how humans **understand/do** things?

Part 1 - General introduction

Part 2 - Image transformation

3 kinds of transformation

Part 3 - Point-to-point transformation

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Part 6 - Quality measure

Part 7 - Machine learning

# Artificial intelligence (AI)

AI applied to images: computer vision

- **System of experts**: **emulates** the decision-making ability of a human expert. (Wikipedia)

**Expert**: specifies all steps he took to make the decision

**Machine**: is programmed such as to **reproduce** the steps.

- **Machine learning** gives "computers the ability to learn without being explicitly programmed." [A. Samuel 59] (Wikipedia)

**Expert**: gives the decision for a set of **training examples**

**Machine**: is programmed such as to **mimic** the decision.

Big interest into machine learning due to deep learning!!

# An example: digit recognition solved with machine learning

Algorithm: nearest neighbor search.



Source: V. Athitsos. Nearest Neighbor Retrieval and Classification.

# Pro's and con's of machine learning

- + efficient... – if many many (training) samples
- expert needs to give decisions for each training data  
**(supervised)**
- there exists **non supervised** (k-means clustering) but less efficient

Today's most efficient machine learning algorithms: **deep learning**.  
Classification with Deep Convolutional Neural Networks by A Krizhevsky won **ImageNet** 2012 challenge with **major decrease** in classification error.

Since then, **tremendous** work in the community on deep learning.

First layers in deep learning... look like classical image processing!!!