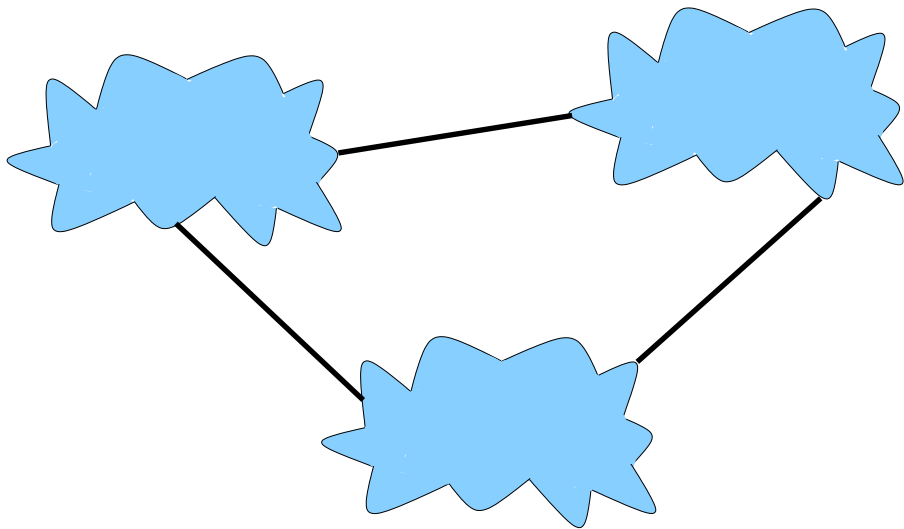


# Monotony in Service Orchestrations

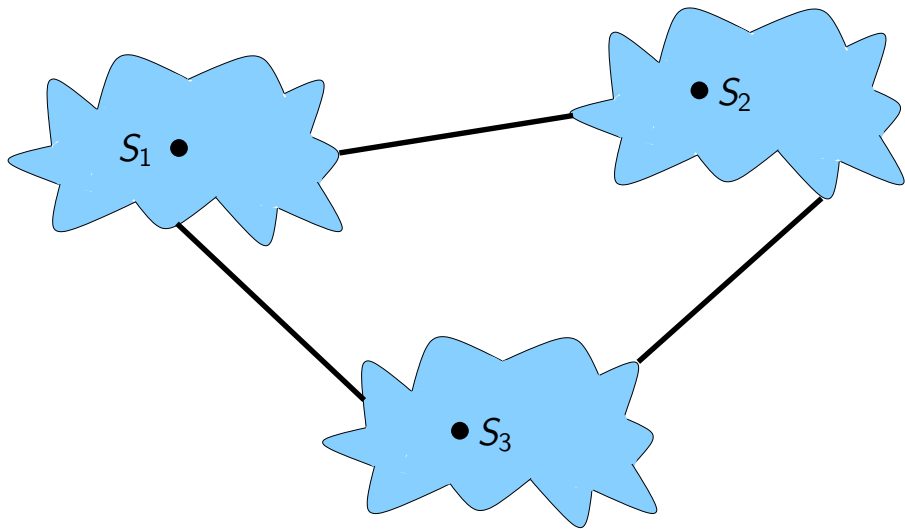
A. Bouillard   S. Rosario   A. Benveniste   S. Haar

# Web Services and Orchestrations

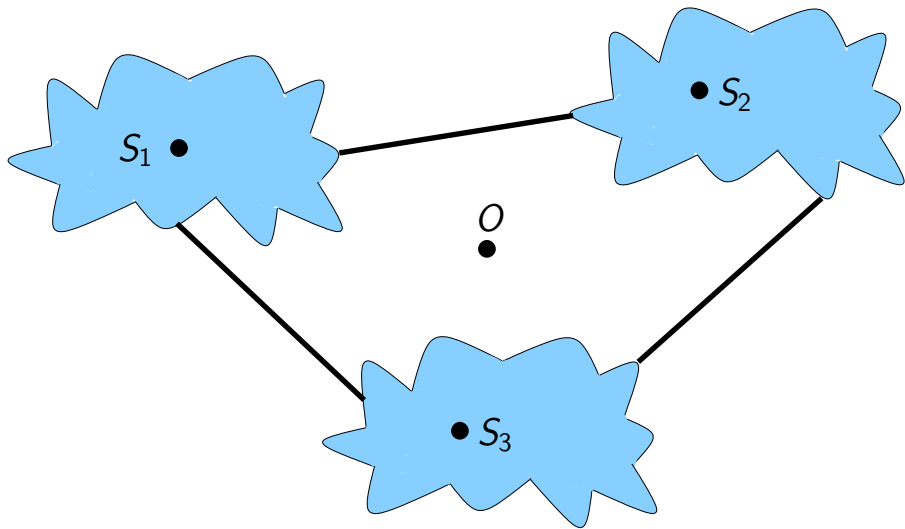
## Web Services and Orchestrations



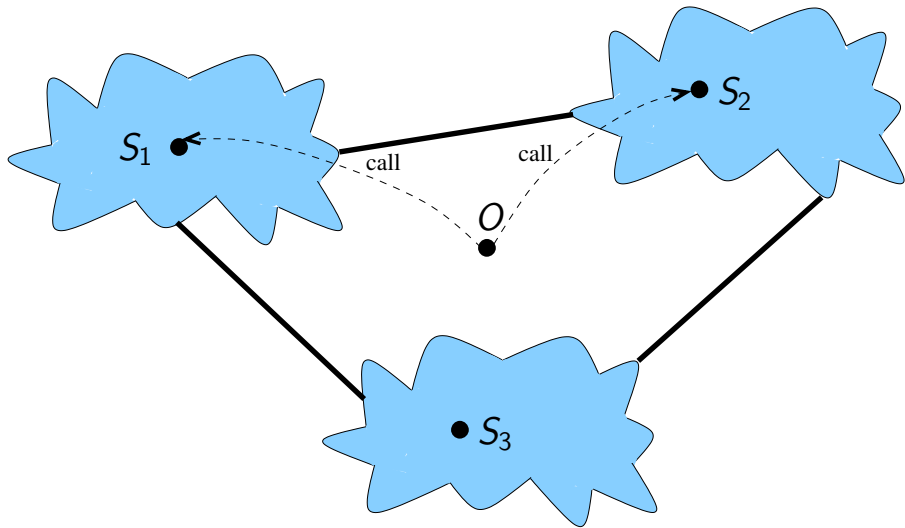
## Web Services and Orchestrations



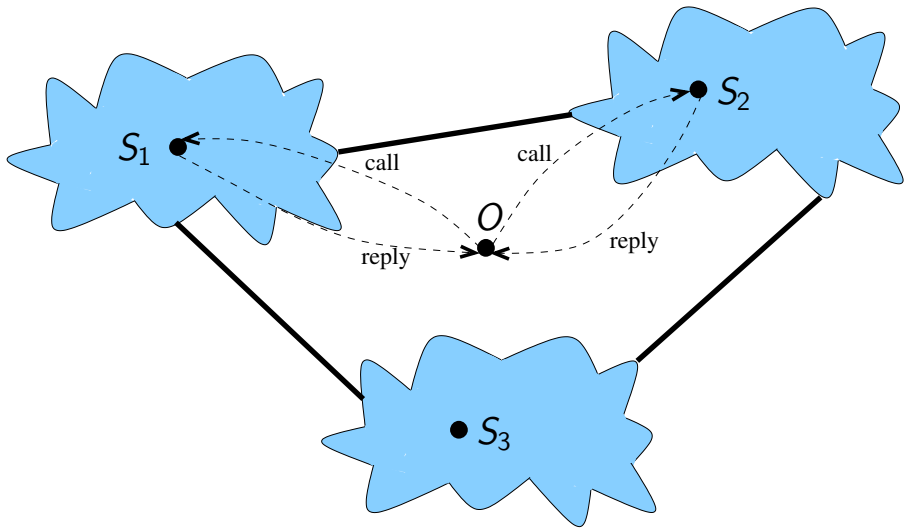
## Web Services and Orchestrations



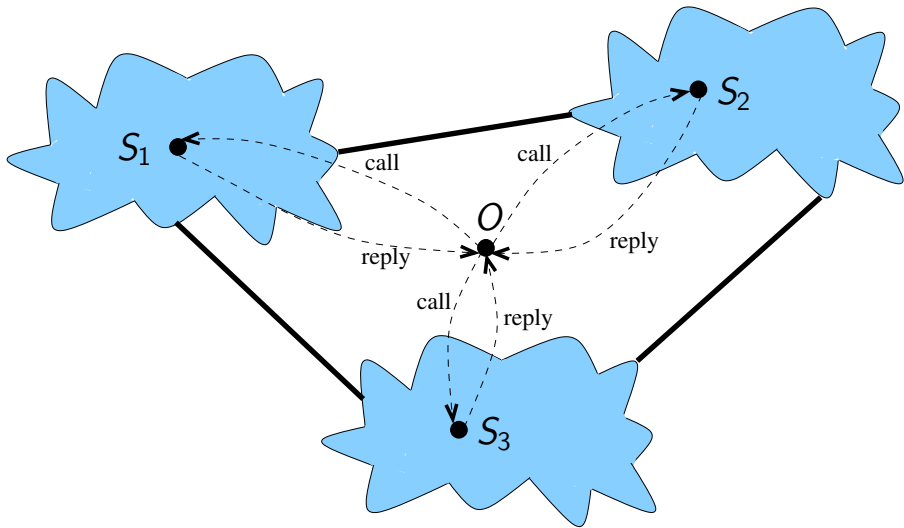
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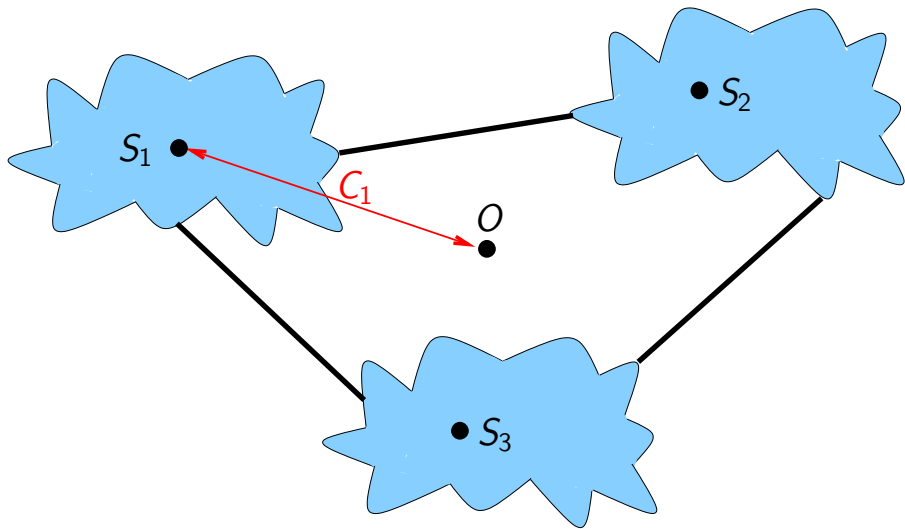


## Web Services and Orchestrations

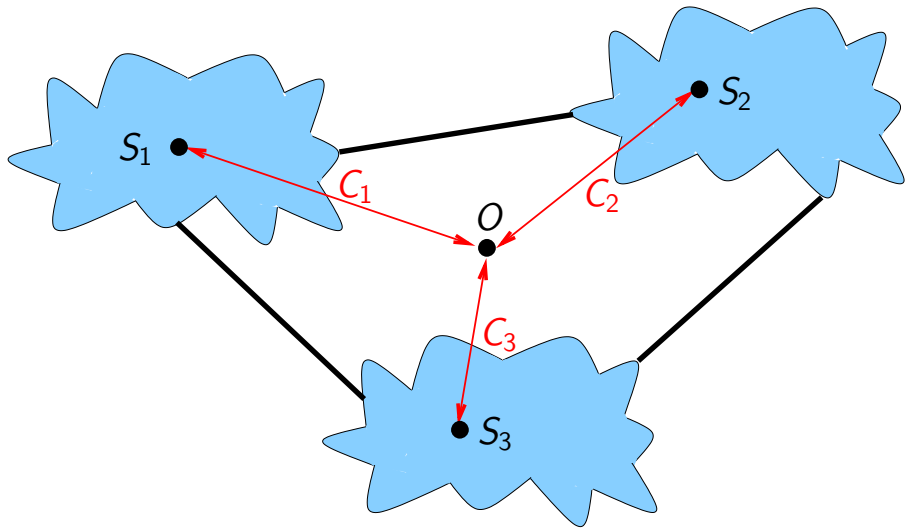




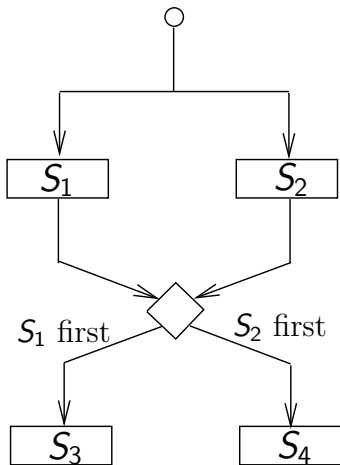
## Contract, Contract Composition



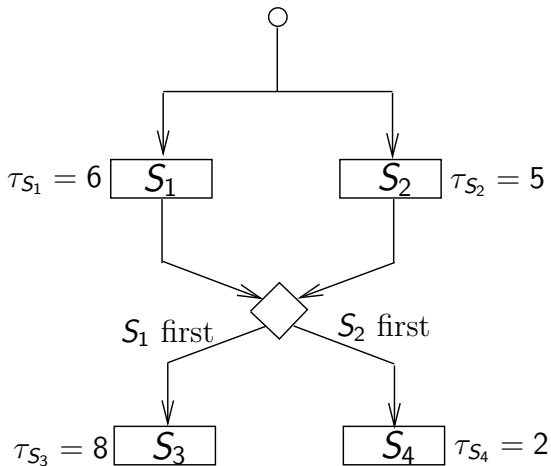
## Contract, Contract Composition



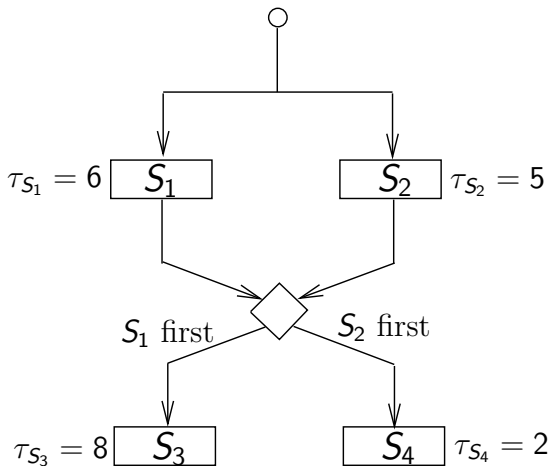
## A non-monotonic orchestration



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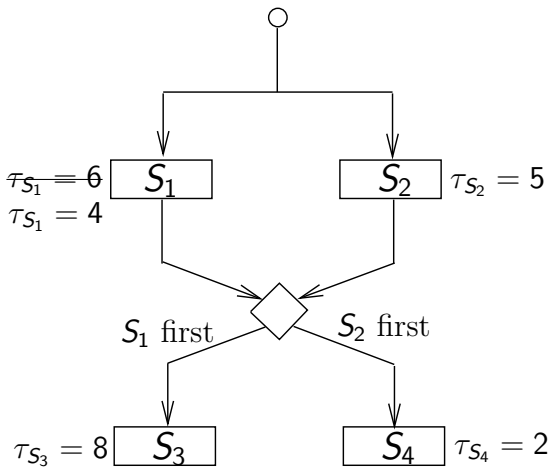


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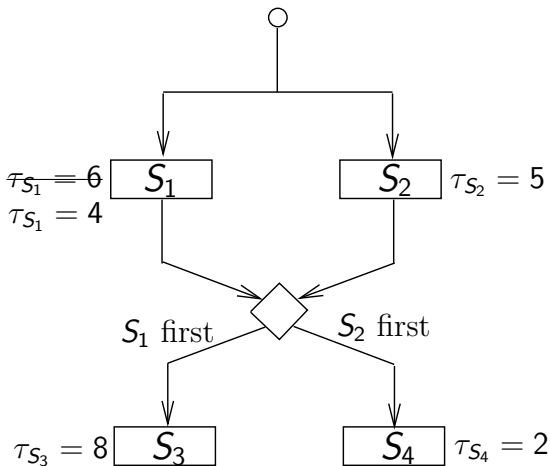


Overall latency :  $\tau_{S_2} + \tau_{S_4} = 7$

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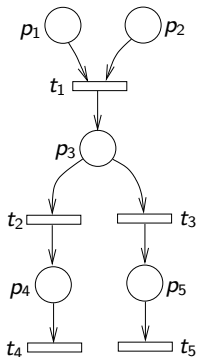


Overall latency :  $\tau_{S_1} + \tau_{S_3} = 12$

**Colored, Occurrence Nets:** to model orchestrations



# Petri Nets



$$N = (\mathcal{P}, \mathcal{T}, \mathcal{F}, M_0)$$

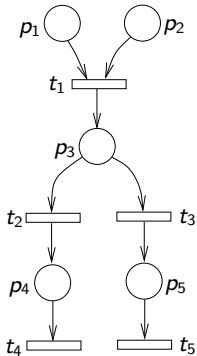
$\mathcal{P}$  : Set of Places

$\mathcal{T}$  : Set of Transitions

$\mathcal{F} \subseteq (\mathcal{P} \times \mathcal{T}) \cup (\mathcal{T} \times \mathcal{P})$  : Flow Relation

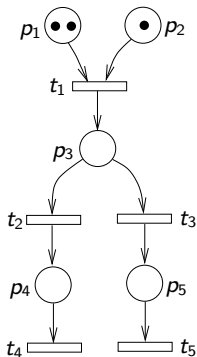
$M_0 : \mathcal{P} \rightarrow \mathbb{N}$ : Initial Marking

# Petri Nets



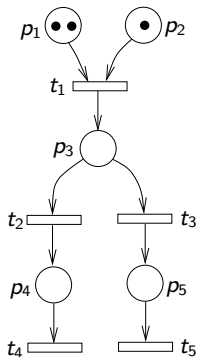
$$M_0 = \{p_1 \rightarrow 2, p_2 \rightarrow 1, p_3 \rightarrow 0 \\ p_4 \rightarrow 0, p_5 \rightarrow 0\}$$

# Petri Nets



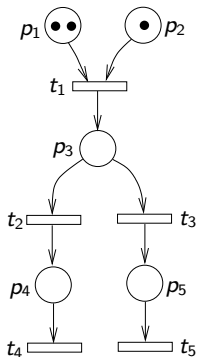
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# Petri Nets



**Preset** of a node  $x$  :  $\bullet x$   
for *e.g.*,  $\bullet t_1 = \{p_1, p_2\}$

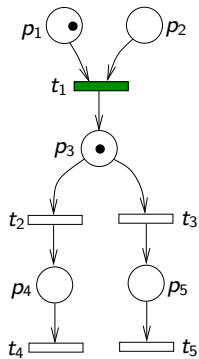
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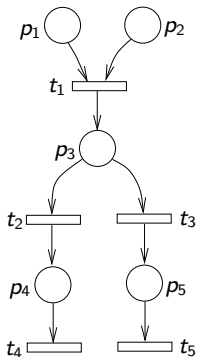
**Postset** of a node  $x$  :  $x^\bullet$   
for *e.g.*,  $t_1^\bullet = \{p_3\}$

# Petri Nets



*Firing of transition  $t_1$*

# Petri Nets

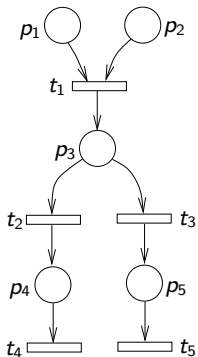


**Causality** Relation :  $\leq$

for e.g. :  $p_3 < t_1 < p_1$

$t_1 < t_2 < t_4$

# Petri Nets



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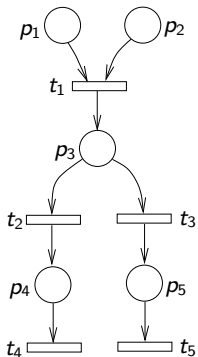
$t_1 < t_2 < t_4$

**Conflict** Relation :  $\#$

for e.g. :  $t_2 \# t_3$



# Petri Nets



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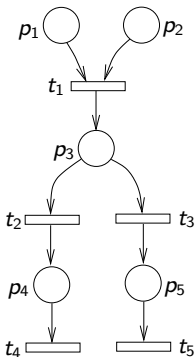
$t_1 < t_2 < t_4$

**Conflict** Relation :  $\#$

for e.g. :  $t_2 \# t_3$

$t_4 \# t_5$

# Petri Nets

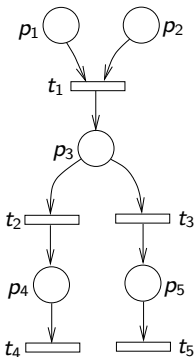


A **configuration** is a sub-net  $\kappa$  s.t.:

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If  $x \in \kappa$  and  $x' < x$ , then  $x' \in \kappa$ .

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If  $x \in \kappa$  and  $x' < x$ , then  $x' \in \kappa$ .
2.  $\kappa$  is conflict-free.  
 $\nexists x, x' \in \kappa$  s.t.  $x \# x'$

## Occurrence Nets

A safe net  $N$  is called an *occurrence net* iff

1. No node of  $N$  is in self-conflict.
2.  $\leq$  is a partial order
3.  $\lceil t \rceil = \{x \in N \mid x \leq t\}$  is finite for all transitions of  $N$ .
4.  $|\bullet p| \leq 1$  for all places of  $N$ .

Our Model: **OrchNets**

# OrchNets

- Tokens have *colors*: (value, date)

# OrchNets

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- A transition  $t$  has functions  $(\phi_t, \tau_t)$  that modify the token colors.

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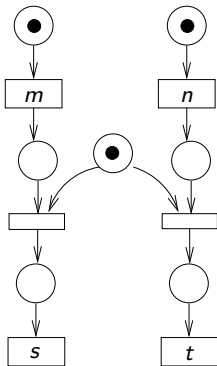
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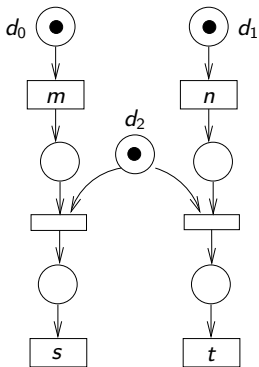
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- $T_{\text{init}} = (\tau_p)_{p \in \text{min}(\mathcal{P})}$  : family of *initial date functions*.

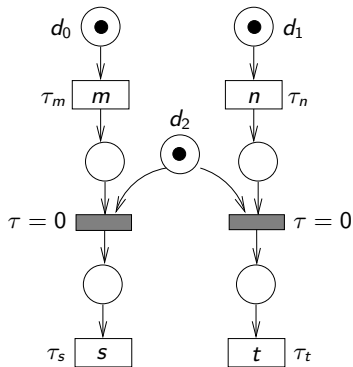
## OrchNets: Example



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# OrchNets: Example



In general,  $\phi_t$  and  $\tau_t$  are non-deterministic functions.

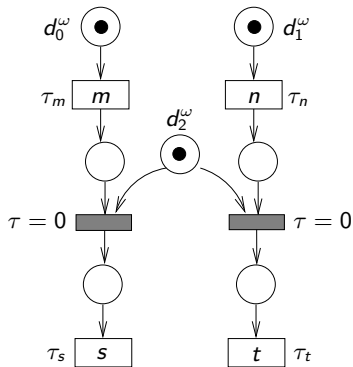


$\omega \in \Omega$ , a **daemon** variable that resolves non-determinism.

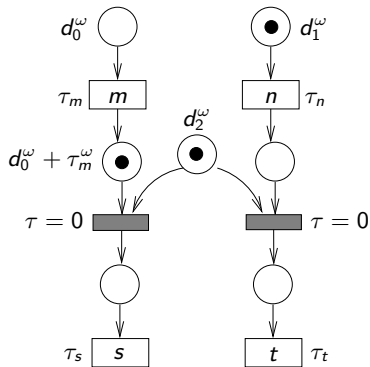
$\omega \in \Omega$ , a **daemon** variable that resolves non-determinism.

For a given value of  $\omega$ ,  $\phi_t^\omega$  and  $\tau_t^\omega$  are deterministic functions.

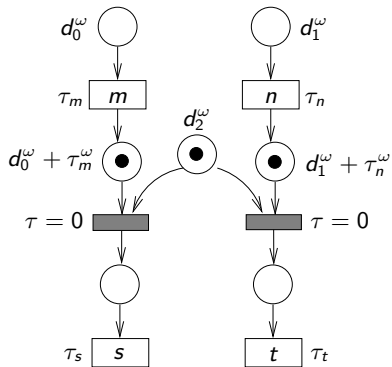
For a fixed  $\omega$



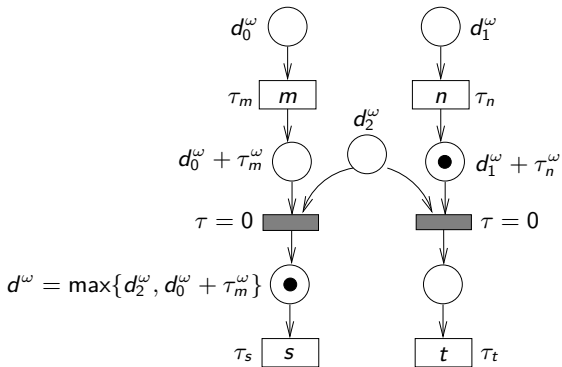
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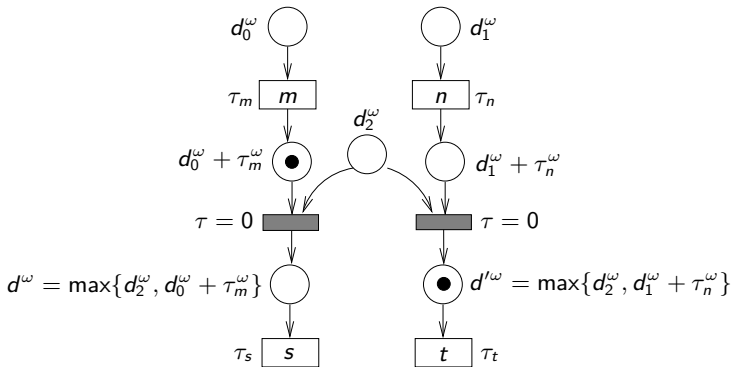
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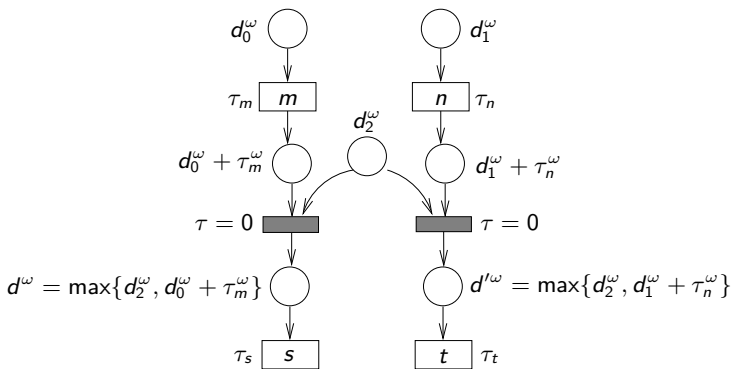
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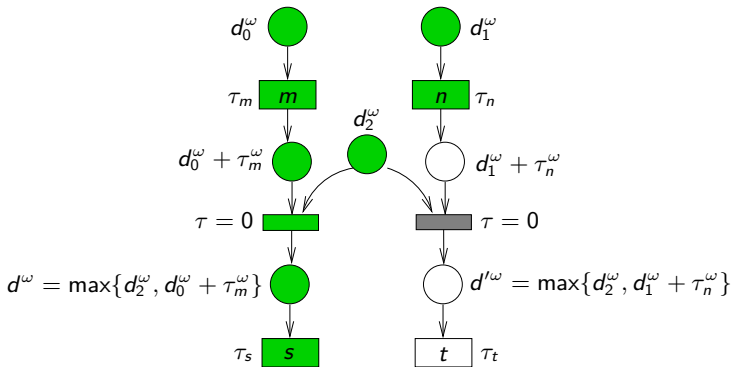


**Actually occurring configuration** for a given  $\omega$ :  $\bar{\kappa}(\mathcal{N}, \omega)$

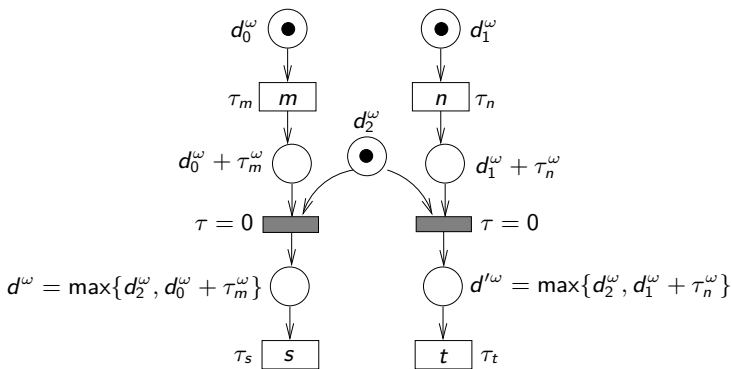


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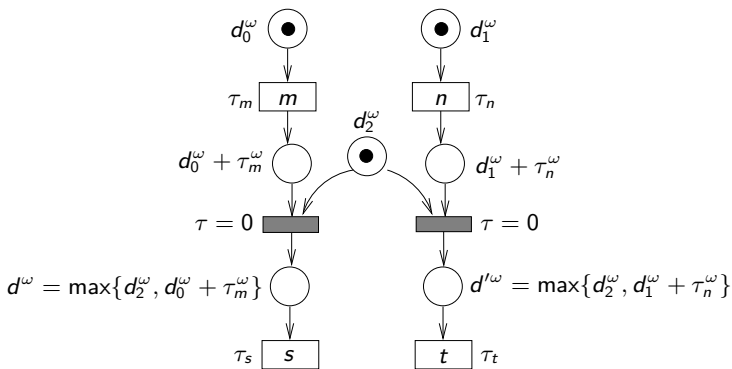
## Execution Time



**Execution Time** of a maximal configuration  $\bar{\kappa}$  of  $\mathcal{N}$ :

$$E_\omega(\bar{\kappa}, \mathcal{N}) = \{\max(d_x^\omega) \mid x \in \bar{\kappa}\}$$

# Execution Time

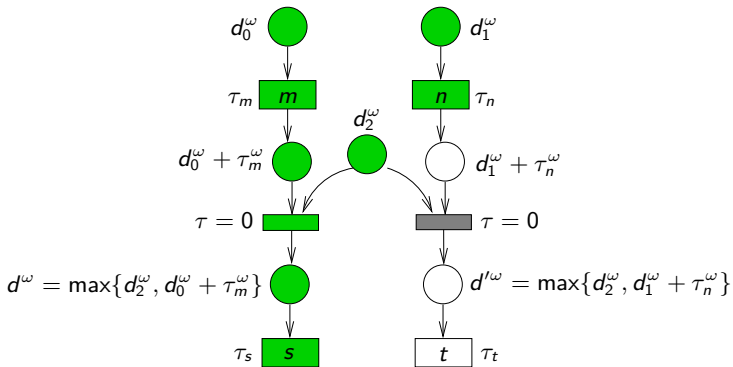


For a given  $\omega$ , **execution time** of  $\mathcal{N}$ :

$$E_\omega(\mathcal{N}) = E_\omega(\bar{\kappa}(\mathcal{N}, \omega), \mathcal{N})$$

When  $d^\omega < d'^\omega$  ..

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$$E_\omega(\mathcal{N}) = d^\omega + \tau_s^\omega$$

Characterising Monotony..

## Pre-Orchnets

Call **pre-OrchNet** a tuple  $\mathbb{N} = (N, \Phi, \mathbb{T}, \mathbb{T}_{\text{init}})$  where,



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3.  $\mathbb{T}_{\text{init}}$ : sets of families of initial date functions  $T_{\text{init}}$ .

Write  $\mathcal{N} \in \mathbb{N}$  if there exists  $T \in \mathbb{T}$  and  $T_{\text{init}} \in \mathbb{T}_{\text{init}}$  s.t.

$$\mathcal{N} = (N, \Phi, T, T_{\text{init}})$$

## Pre-Orchnets: Order Relation

For two families  $T$  and  $T'$  of latency functions, write

$$T \geq T'$$

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For  $\mathcal{N}, \mathcal{N}' \in \mathbb{N}$ , write

$$\mathcal{N} \geq \mathcal{N}'$$

if  $T \geq T'$  and  $T_{\text{init}} \geq T'_{\text{init}}$  both hold.

## Monotony: Definition



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Pre-Orchnet  $\mathbb{N} = (N, \Phi, \mathbb{T}, \mathbb{T}_{\text{init}})$  is called **monotonic** if,  
 $\forall \mathcal{N}, \mathcal{N}' \in \mathbb{N}$  s.t.  $\mathcal{N} \geq \mathcal{N}'$ ,

$$E_{\omega}(\mathcal{N}) \geq E_{\omega}(\mathcal{N}')$$

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$$\begin{aligned} E_{\omega}(\mathcal{N}') &= E_{\omega}(\bar{\kappa}(\mathcal{N}', \omega), \mathcal{N}') \geq E_{\omega}(\bar{\kappa}(\mathcal{N}', \omega), \mathcal{N}) \\ &\geq E_{\omega}(\bar{\kappa}(\mathcal{N}, \omega), \mathcal{N}) = E_{\omega}(\mathcal{N}) \end{aligned}$$

## A Necessary Condition ..



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If the sufficient condition

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is violated,

## A Necessary Condition ..

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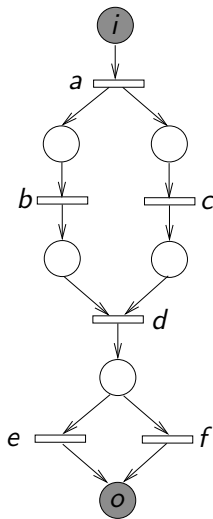
is violated, and for any two OrchNets  $\mathcal{N}, \mathcal{N}'$  s.t  $\mathcal{N} \in \mathbb{N}$ ,

$$\mathcal{N}' \geq \mathcal{N} \implies \mathcal{N}' \in \mathbb{N}$$

holds, then  $\mathbb{N}$  is not monotonic.

A structural condition for monotony...

## Workflow nets (WFnets)



We consider safe WF nets, without any loops.

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$(W,$

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$(W, \Phi, \mathbb{T}, \mathbb{T}_{\text{init}}) : \textit{pre-WFnet}$

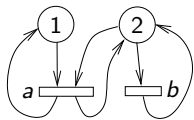
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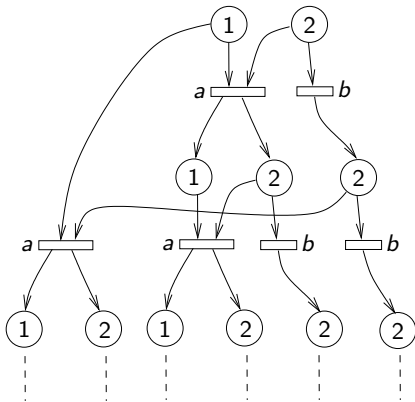
Unfolding  $W$  gives the occurrence net  $N_W$  and a corresponding Orchnet

$$(N_W, \Phi_W, \mathbb{T}_W, \mathbb{T}_{\text{init}})$$





$N$



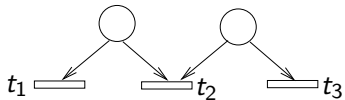
$U_N$

## Clusters.

For a safe net  $N$ , a *cluster* is a minimal set  $\mathbf{c}$  of places and transitions of  $N$  such that

$$\forall t \in \mathbf{c} \implies \bullet t \subseteq \mathbf{c} \quad , \quad \forall p \in \mathbf{c} \implies p^\bullet \subseteq \mathbf{c}$$

# Clusters



$t_1, t_2, t_3$  are in the same cluster

## Sufficient Condition for Monotony of WFnets

$W$ : WFnet,  $N_W$ : unfolding of  $W$ .

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$$\forall t_1, t_2 \in c, t_1 \neq t_2 \implies t_1^\bullet = t_2^\bullet$$

Only a very restricted class of nets are indeed monotonic.

## Conditional Monotony..

Conditional Monotony: Compare execution times only for identical responses.



## In Conclusion..

- Identified and defined the problem of monotony in service compositions.
- Insights and reconsideration into the formulation of contracts.

## Future Work..

- Extend the notion of monotony to probabilistic contracts.

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- Extend the notion of monotony to probabilistic contracts.
- Consider more, QoS parameters in our study.

Thank you..