

# Polylib : A Library for Computations on Polyhedra

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# Outline

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## Polylib Introduction

- A library for doing operations on unions of Polyhedra
- Useful for doing program restructuring transformations in parallelizing compilers
- Used for defining domains of variables in SARE
- Allows computation of useful information in a loop nest
- A tool to study polyhedra and other related mathematical objects

## Previous Work on Polylib

- First developed at IRISA in connection with the ALPHA project in 1993
- Two independent versions : IRISA Polylib & Strasbourg Polylib
- Another Similar Library - NewPolka - developed at VERIMAG

## Basic Features

- Mathematical objects: Polyhedra, Matrices, Vectors
- Polyhedral operations : Union, Intersection, Difference, Simplify, Image and PreImage, etc . . .
- Parametric Polyhedra Representation
- Ehrhart Polynomial Computations
- Z-Polyhedra and Lattices
- Options to support 32/64 bits or multi-precision integers

## Few Definitions on Polyhedra

- Dual representation of Polyhedra

$$\{ X \mid AX = b, CX \leq d \} \equiv \{ X \mid X = L \lambda + R \mu + V \vartheta \}$$

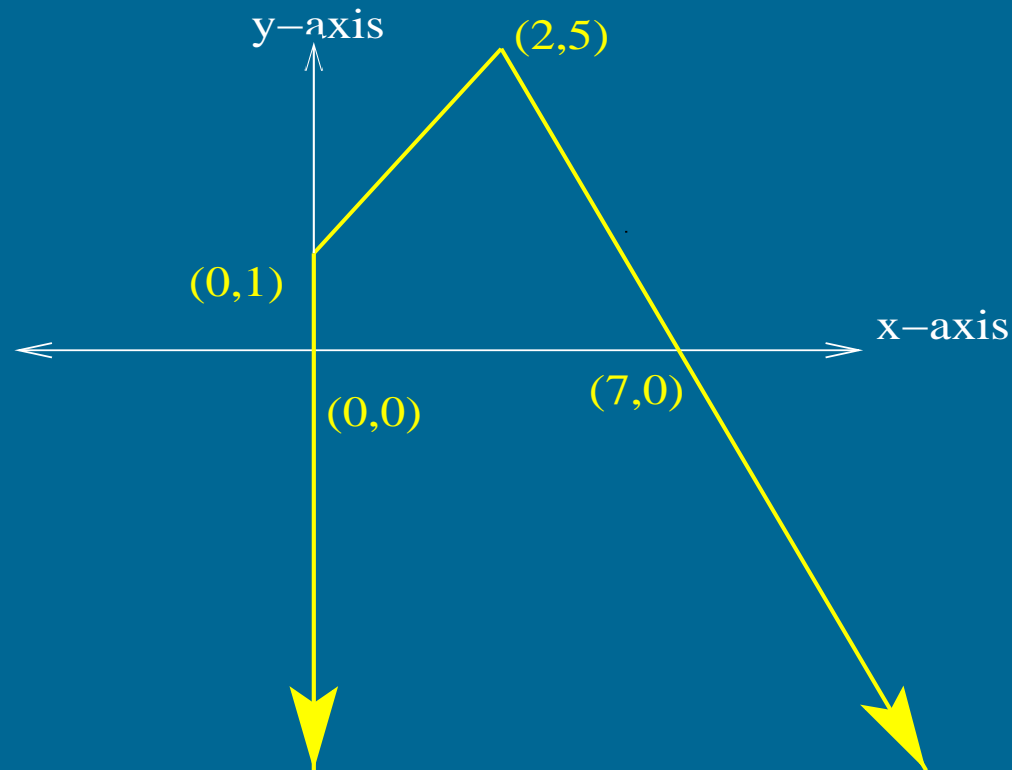
- Computation of Dual representations

  - Chernikova Algorithm

- Parametrized Polyhedra Representation

$$\{ X \mid AX \leq BN + C \} \equiv \{ X \mid X = L \lambda + R \mu + V \vartheta \}$$

## Example



**A Polyhedron described by**

**Vertex Set:  $\{(0,1), (2,5)\}$**

**Uni-directional Ray set:  $\{(0,-1), (1,-1)\}$**

## Lattices and Z-polyhedron

- **Lattice** - A set consisting of all the linear integral combinations of basis vectors. That is,

$$L(A) = \{ Y \in \mathbb{R}^m \mid Y = AX, A \in \mathbb{Q}^{m \times n}, X \in \mathbb{Z}^n \}$$

- **Z-Polyhderon** - An intersection of a polyhderon and an integral full dimensional lattice.

# Ehrhart Polynomials

- Used in the enumeration of lattice points in a Polyhedron
- Useful in analyzing nested loops to derive efficient parallel programs
- **Definitions :**
  - **Periodic Number:**  $[n_1, n_2, \dots, n_q]_{\mathbb{N}}$   
Example:  $(-1)^n = [1, -1]_n$

## Current Work and Progress

- Unifying the two independent versions into a single new Polylib
- To support options for 32 bits, 64 bits and multi-precision integers
- Merging Ehrhart and Z-polyhedron part into the new version
- Assisting in the integration of Polylib with MMALPHA
- Extending the portability of Polylib to Win 2000/NT

## Future development of Polylib

- A large set of test suits
- A user friendly/graphical interface
- Options to support 32 bits, 64 bits and multi precision integers in MMALPHA

**Thank You**